

1. Consider the vectors: $\mathbf{a} = \langle 1, 0, -1 \rangle$ $\mathbf{b} = \langle 1, 1, 1 \rangle$ $\mathbf{c} = \langle -1, 1, 0 \rangle$.

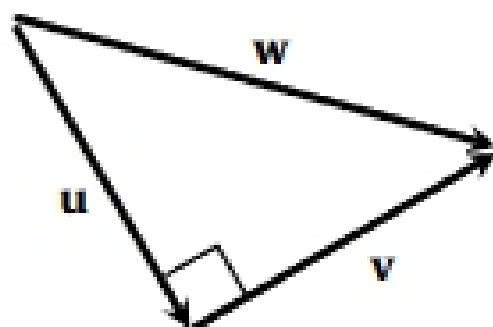
(a) Compute $\mathbf{a} \times \mathbf{b}$. (3 points)

$$\mathbf{a} \times \mathbf{b} = \langle \quad , \quad , \quad \rangle$$

(b) Compute the volume of the parallelepiped determined by the vectors \mathbf{a} , \mathbf{b} , and \mathbf{c} . (2 points)

Volume =

2. Given that \mathbf{u} and \mathbf{v} in the picture at left have length 1, compute $\mathbf{u} \cdot \mathbf{v}$, $\mathbf{u} \cdot \mathbf{w}$, and $\text{proj}_{\mathbf{v}} \mathbf{w}$. (1 point each)



$$\mathbf{u} \cdot \mathbf{v} =$$

$$\mathbf{u} \cdot \mathbf{w} =$$

$$\text{proj}_{\mathbf{v}} \mathbf{w} =$$

3. A particle moves with constant velocity $\langle 3, 1, -1 \rangle$ starting from the point $(3, 2, 4)$ at time $t = 0$. When and where will it cross the xy -plane? (3 points)

When: $t =$

Where: (\quad , \quad , \quad)

4. Let A be the plane given by $x - z = 1$ and B the plane given by $x + y + z = 2$.

(a) Find a normal vector \mathbf{n} for the plane A . (1 points)

$$\mathbf{n} = \langle \quad , \quad , \quad \rangle$$

(b) Find the angle between the two planes. (2 points)

$$\theta =$$

(c) Find the equation of a plane C which is perpendicular to both A and B . (3 points)

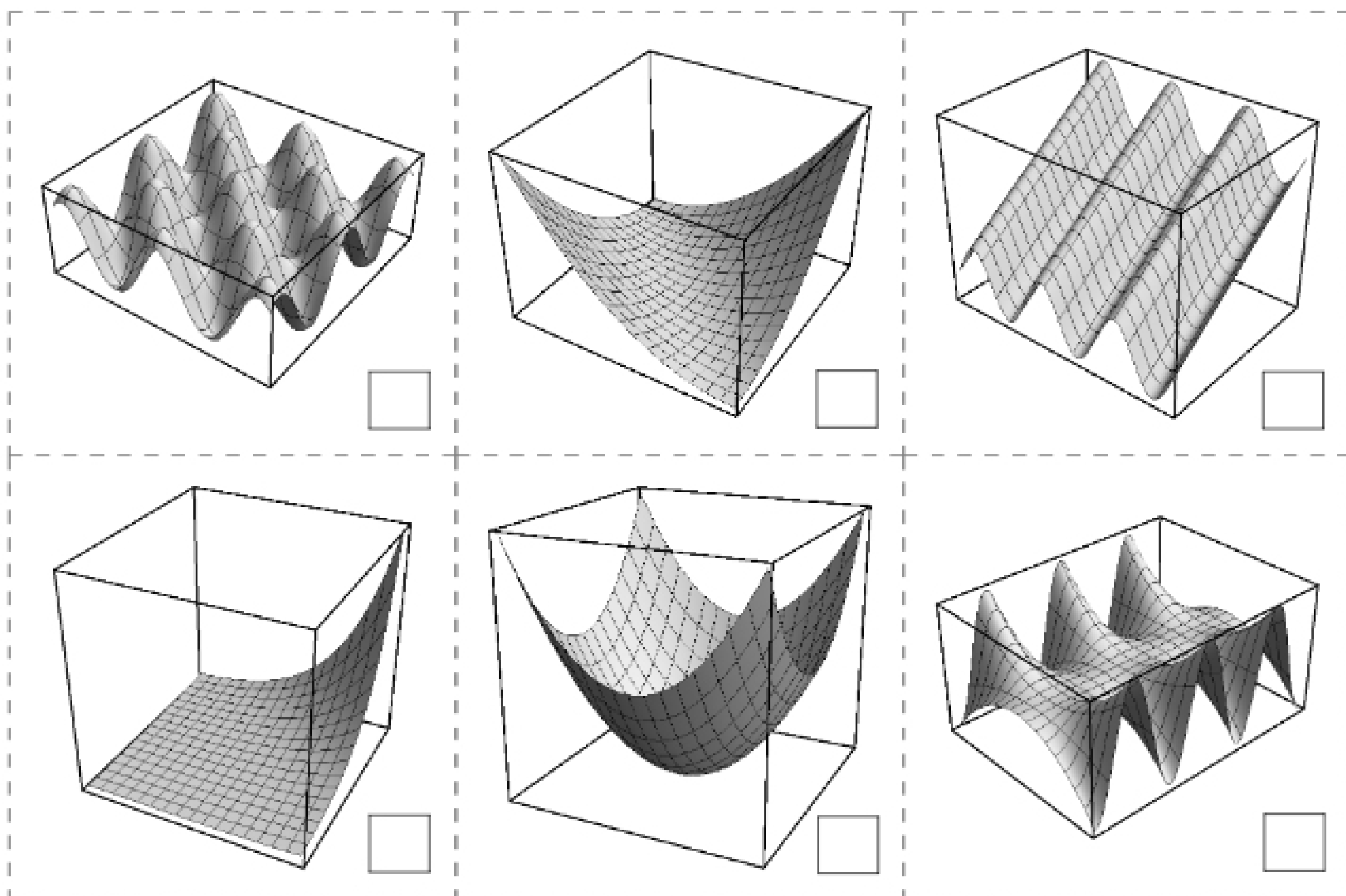
Equation: $\square x + \square y + \square z = \square$

5. Exactly one of the following two limits exists. Circle the one that exists and justify your answer. (5 points)

$$\lim_{(x,y) \rightarrow (0,0)} \left(\frac{x^2 - y^2}{\sqrt{x^2 + y^2}} \right)$$

$$\lim_{(x,y) \rightarrow (0,0)} \left(\frac{xy}{(x^2 + y^2)^2} \right)$$

6. For each function label its graph from among the options below: (a) $(x+y)^2$ (b) $x+\cos(y)$
 (3 points each)



7. Circle the equation for the quadratic surface shown at right. (3 points)

- (a) $x^2 + y^2 + z^2 = 1$
- (b) $x^2 - y^2 - z^2 = -1$
- (c) $x^2 + y^2 - z^2 = -1$
- (d) $x^2 - y^2 - z^2 = 1$
- (e) $x - y^2 - z^2 = 1$

