

# CSE 543 - Computer Security

Lecture 5 - Cryptography II

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URL: <http://www.cse.psu.edu/~tjaeger/cse543-f06/>

# RSA (Rivest, Shamir, Adelman)

- A dominant public key algorithm
  - The algorithm itself is conceptually simple
  - Why it is secure is very deep (number theory)
  - Use properties of exponentiation modulo a product of large primes

"A method for obtaining Digital Signatures and Public Key Cryptosystems", Communications of the ACM, Feb., 1978 21(2) pages 120-126.



# RSA Key Generation

- Pick two large primes  $p$  and  $q$
- Calculate  $n = pq$
- Pick  $e$  such that it is relatively prime to  $\phi(n) = (q-1)(p-1)$ 
  - “Euler’s Totient Function”
- $d \approx e^{-1} \pmod{\phi(n)}$   
or  
 $de \pmod{\phi(n)} = 1$

1.  $p=3, q=11$
2.  $n = 3*11 = 33$
3.  $\phi(n) = (2*10) = 20$
4.  $e = 7 \mid \text{GCD}(20,7) = 1$   
“Euclid’s Algorithm”
5.  $d = 7^{-1} \pmod{20}$   
 $d = 7 \pmod{20} = 1$   
 $d = 3$

