

Chapter 9

Algorithm Efficiency &

Programming efficiency ~~Sorting~~ has been important up to this point, but we're now going to examine the methods that have been developed to determine just how efficient a program is.

- ✓ **Measuring Algorithm**

- ✓ **Efficiency**

- ✓ **Example: Searching**

- ✓ **Algorithms**

- ✓ **Example: Sorting Algorithms**

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32

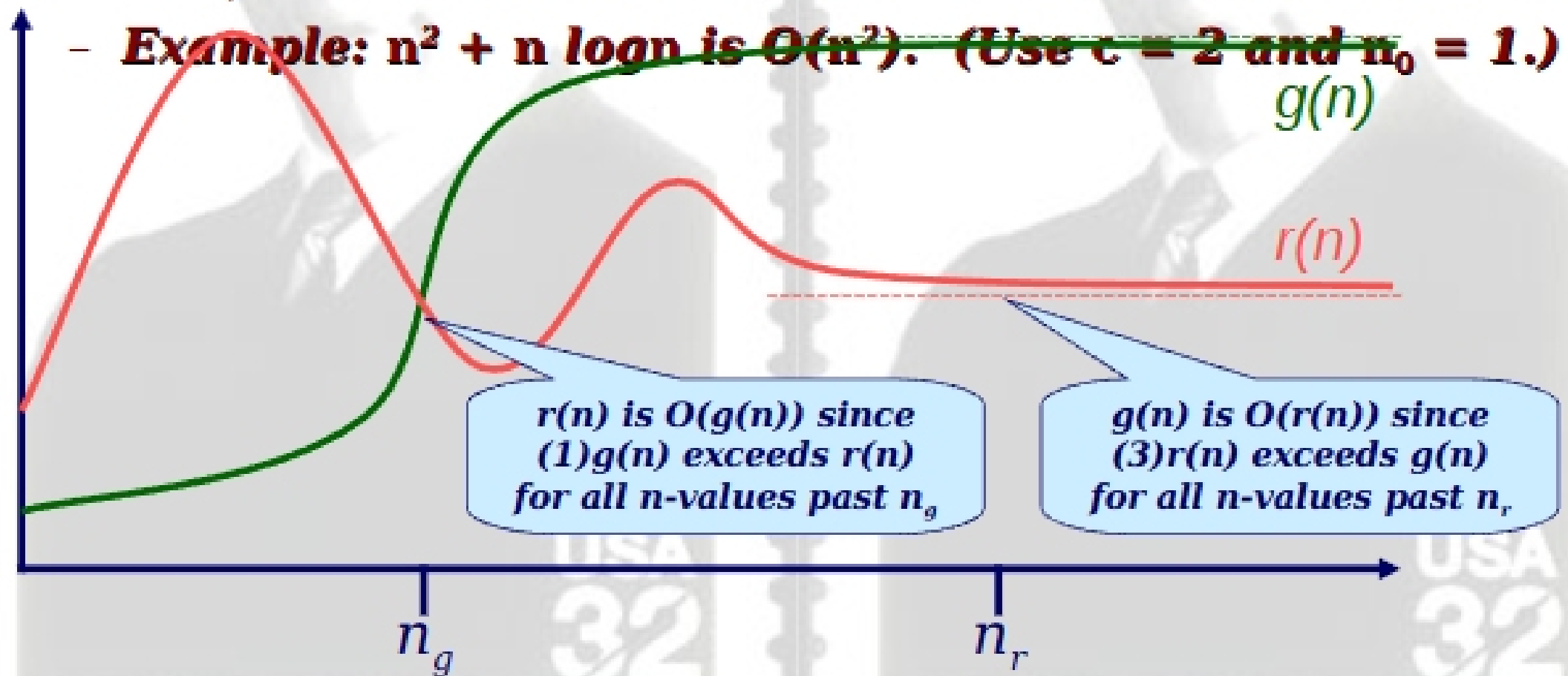
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Time Complexity Terminology: Big-O

- **Function $T(n)$ is said to be $O(f(n))$ if there are positive constants c and n_0 such that $T(n) \leq c f(n)$ for every $n \geq n_0$.**
 - **Example: $n^3 + 3n^2 + 6n + 5$ is $O(n^3)$. (Use $c = 15$ and $n_0 = 1$.)**
 - **Example: $n^2 + n \log n$ is $O(n^2)$. (Use $c = 2$ and $n_0 = 1$.)**



Demonstrating The Big-O Concept

Both algorithms below have $O(n^3)$ time complexity.

		ALGORITHM	
		A	B
Input Size n	10	1,110	11,110
	100	1,010,100	2,010,100
	1,000	1,001,001,000	1,101,001,000
	10,000	1,000,100,010,000	1,010,100,010,000
	100,000	1,000,010,000,100,000 1,000,001,000,001,000,000	1,001,010,000,100,000 1,000,101,000,001,000,000
	1,000,000	1,000,001,000,000,000,000 0	1,001,001,000,000,000,000 0

(In fact, the execution time for Algorithm A is $n^3 + n^2 + n$, and the execution time for Algorithm B is $n^3 + 101n^2 + n$.)