

## Chapter 6

-Approaches to Assigning Probabilities:

- **Classical approach:** based on equally likely events
- **Relative frequency:** assigning probabilities based on experimentation or historical data
- **Subjective approach:** assigning probabilities based on the assignor's judgment (ex: weather forecast)

-Complement of an event:  $1 - P(\text{event occurring})$

-Joint probability: intersection of events (A and B)

-Union of two events: event containing all sample points in A or B or both.

-Mutually Exclusive Events: two events cannot occur together (joint probability is 0); no points in common  $a = 2, b = 5$

-Marginal probabilities: computed by adding across rows and down columns; calculated in the margins

	B <sub>1</sub>	B <sub>2</sub>	P(A)
A <sub>1</sub>			
A <sub>2</sub>			
P(B)			1.00

-Conditional probabilities: used to determine how two events are related =  $P(A|B) = \frac{P(A \cap B)}{P(B)}$

-Independence:  $P(A|B) = P(A)$

-Multiplication Rule:  $P(A \cap B) = P(A|B) \cdot P(B)$

-Addition Rule:  $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

## Chapter 7

-Discrete Random Variable: one that takes on a **countable** number of values

-Continuous Random Variable: one whose values are **not countable**. Ex: time (30.1 minutes, 30.10000001 minutes, etc.)

Discrete Probability:

-represent a **population** so use describe them using various parameters:

$$E(X) = \mu = \sum xP(x) : \text{weighted average/population mean}$$

$$V(X) = \sigma^2 = \sum x^2 P(x) - \mu^2 : \text{variance}$$

$$\sigma = \sqrt{\sigma^2} : \text{standard deviation}$$

**Laws of Expected Value:**

$$E(c) = c$$

$$E(X + c) = E(X) + c$$

$$E(cX) = cE(X)$$

**Laws of Variance:**

$$V(c) = 0$$

$$V(X + c) = V(X)$$

$$V(cX) = c^2V(X)$$

Bivariate Distributions:

-Covariance:  $COV(X, Y) = \sum x \sum y xyP(x, y) - \mu_x \mu_y$

-Coefficient of Correlation:  $\rho = \frac{COV(X, Y)}{\sigma_x \sigma_y}$

-Laws:

$$E(X + Y) = E(X) + E(Y)$$

$$V(X + Y) = V(X) + V(Y) + 2COV(X, Y) \quad \text{If X and Y are independent, } COV(X, Y) = 0 \text{ and thus } V(X + Y) = V(X) + V(Y)$$

Binomial Random Variable: counts the number of successes in n trials of the binomial experiment.

$$P(X) = \frac{n!}{x!(n-x)!} p^x q^{n-x}$$

Binomial Distribution:

$$\mu = np$$

$$\sigma^2 = np(1-p)$$

$$\sigma = \sqrt{np(1-p)}$$

Poisson Experiment: discrete probability distribution that refers to the number of events (successes) within a specific time period or region of space (number of flaws in cloth, number of accidents in one day on a particular highway, etc.)

$$P(x) = \frac{e^{-\mu} \mu^x}{x!}$$

## Chapter 8

### Continuous Random Variables

#### -Probability Density Functions

$$f(x) = 1/b-a \text{ where } a < x < b$$

$$\text{example: } P(2500 < x < 3000) = (3000-2500) \times 1/b-a$$

-Normal Distribution: bell shaped and symmetrical around the mean

-  $Z = X - \text{mean} / \text{standard deviation}$

-Exponential Distribution:  $\lambda e^{-\lambda x} \quad x > 0$

-Student t distribution:  $v(\text{nu}) = \text{degrees of freedom}$  and gamma is k value

-Chi-square distribution is not symmetrical

-F Distribution: density function, which has 2 v's and degrees of freedom in numerator and denominator

## Chapter 9

Sampling Distribution: distribution created by sampling

$$\text{Mean} = \mu \quad \text{Variance} = \sigma^2/n \quad \text{Standard deviation} = \sigma/\sqrt{n} \quad Z = \frac{\text{xbar} - \mu}{\sigma/\sqrt{n}}$$

### Central Limit Theorem:

-Sampling distribution of the mean of a random sample drawn from any population is approximately normal for sufficiently large sample size (30)

-If the population is normal, then xbar is normally distributed for all values of n

If it is non-normal then it is approximately normal for only larger values of n.

Example:

$$P(\text{Xbar} > 32) = P\left(\frac{\text{xbar} - \mu}{\sigma} > \frac{\text{expected} - \text{mean}}{\text{standard deviation}}\right) = P(Z > \#)$$

### Sampling Distribution of a Proportion

-Count the number of successes in a sample and compute:  $\text{Phat} = X/n$

$$\mu = np \quad \sigma = \sqrt{p(1-p)/n} \quad (\text{Square root of whole thing})$$

Phat is the standard error of proportion