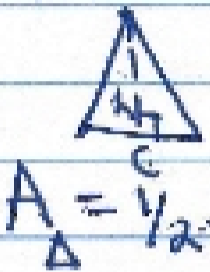
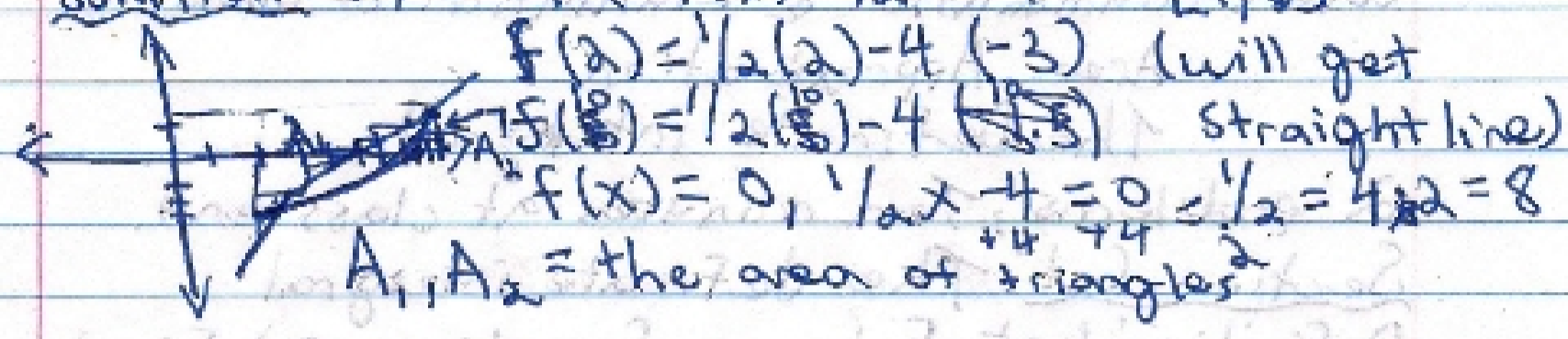


an appropriately chosen function.

Solution: 1.) Graph  $f(x) = \frac{1}{2}x - 4$  on  $[a, 10]$



Then what is  $\int_a^{10} (\frac{1}{2}x - 4) dx = \{A_1, -A_2\} = 1 - 9 = -8$

3.) Find  $A_1$  &  $A_2$

$$A_1 = \frac{1}{2} \cdot 2 \cdot 1 = 1 \text{ units}^2$$

$$A_2 = \frac{1}{2} \cdot 6 \cdot 3 = 9 \text{ units}^2$$

### Algebraic Properties of definite integrals

Let  $f$  &  $g$  be integrable functions on  $[a, b]$

1.)  $\int_a^a f(x) dx = 0$  because  $\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i^*) \Delta x$

$$f(x_i^*) \Delta x \left( \frac{a-a}{n} \right) = 0$$

2.)  $\int_a^b f(x) dx = - \int_b^a f(x) dx$  because  $\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i^*) \Delta x$

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i^*) \Delta x \left( \frac{b-a}{n} = -\frac{(a-b)}{n} \right) = - \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i^*) \Delta x$$

$$\frac{a-b}{n} = - \int_b^a f(x) dx$$

3.)  $\int_a^b k \cdot f(x) dx = k \cdot \int_a^b f(x) dx$

( $k$  is constant,  $\neq 0$ )

4.)  $\int_a^b (f(x) + g(x)) dx = \int_a^b f(x) dx + \int_a^b g(x) dx$

5.) Suppose  $f$  is integrable over the interval containing points  $a, b$ , &  $c$ ,

$$\int_a^c f(x) dx = \int_a^b f(x) dx + \int_b^c f(x) dx$$

$$\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$$