

# Binomial Coefficients

CS/APMA 202

Rosen section 4.4

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# Binomial Coefficients

- It allows us to do a quick expansion of  $(x+y)^n$
- Why it's really important:
- It provides a good context to present proofs
  - Especially combinatorial proofs

# Review: corollary 1 from section 4.3

• Let  $n$  and  $r$  be non-negative integers with  $r \leq n$ . Then  $C(n, r) = C(n, n-r)$

• Or,

$$\begin{array}{|c|} \hline n \\ \hline \\ \hline r \\ \hline \end{array} = \begin{array}{|c|} \hline n \\ \hline \\ \hline n-r \\ \hline \end{array}$$

• Proof (from last slide set):

$$C(n, r) = \frac{n!}{r!(n-r)!}$$

$$C(n, n-r) = \frac{n!}{(n-r)![n-(n-r)]!} = \frac{n!}{r!(n-r)!}$$