

Light of wavelength 589 nm in vacuum passes through a piece of quartz (crystal of SiO₂) with n=1.458

(a) Speed of light in quartz:

$$v = \frac{c}{n} = \frac{3.0 \times 10^8}{1.458} = 2.06 \times 10^8 \text{ m/s}$$

(b) Wavelength of this light in quartz

$$\lambda = \frac{\lambda_0}{n} = \frac{589}{1.458} = 404 \text{ nm}$$

(c) Frequency: $f = \frac{c}{\lambda_0} = \frac{3.0 \times 10^8}{589 \times 10^{-9}} = 5.09 \times 10^{14} \text{ Hz}$

Example $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$

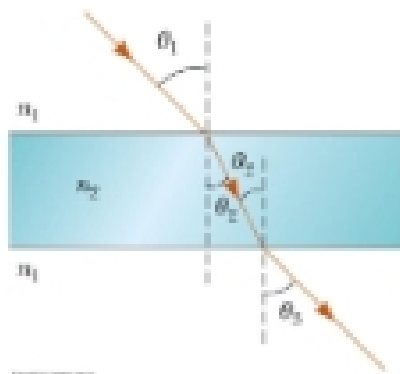
What is the relation between θ_1 and θ_2 ?

(a) $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$

(b) $n_2 \sin(\theta_2) = n_2 \sin(\theta_2)$

Therefore,

$$\begin{aligned} \sin(\theta_1) &= \sin(\theta_2) \\ \Rightarrow \theta_1 &= \theta_2 \end{aligned}$$



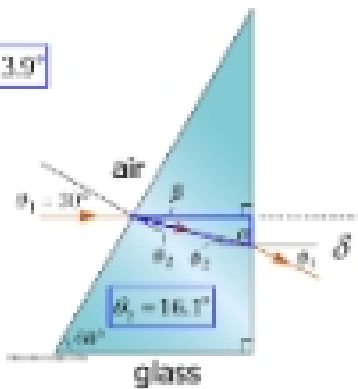
(b) Incident angle ϕ_2
Observation: $\phi_2 = \beta$

Since $\beta = 30^\circ - \theta_2 = 13.9^\circ$ $\phi_2 = \beta = 13.9^\circ$

(c) Calculate θ_1

$$\begin{aligned} \sin(\theta_1) &= \frac{n_2 \sin(\theta_2)}{n_1} \\ &= \frac{1.5 \times \sin(13.9^\circ)}{1.0} \\ &= 0.432 \end{aligned}$$

$$\theta_1 = \sin^{-1}(0.432) = 25.6$$



In this case, ϕ_1 is the same as the deviation angle δ . Please repeat the calculations for red light (n=1.5).

Find the energy of the following. Express your answers in units of electron volts, noting that $1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$.

(a) a photon having a frequency of $2.20 \times 10^{17} \text{ Hz}$

= _____ eV

(b) a photon having a wavelength of 740 nm

= _____ eV

The expression for energy of photon

$$E = h\nu$$

Or

$$E = \frac{hc}{\lambda}$$

Here

h = Planck's constant

c = Speed of light

ν = Frequency of light

λ = Wavelength of light

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$$

a) The energy of a photon having a frequency of $2.20 \times 10^{17} \text{ Hz}$

$$\begin{aligned} E &= h\nu \\ &= 6.626 \times 10^{-34} \times 2.20 \times 10^{17} \\ E &= 1.4577 \times 10^{-16} \text{ J} \end{aligned}$$

In eV

$$\begin{aligned} E &= \frac{1.4577 \times 10^{-16}}{1.6 \times 10^{-19}} \\ E &= 911.06 \text{ eV} \end{aligned}$$

Example $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$

Calculate refraction angle θ_2

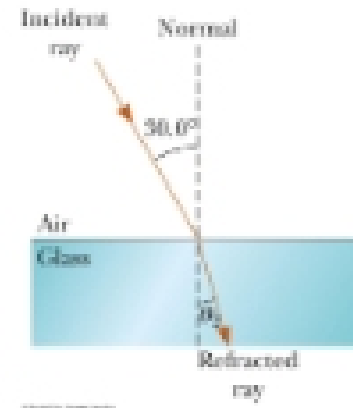
$n=1.00, n_2=1.52$ for $\lambda_0=589 \text{ nm}$

$$n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$$

$$\Rightarrow \sin(\theta_2) = \frac{n_1 \sin(\theta_1)}{n_2}$$

$$\Rightarrow \sin(\theta_2) = \frac{1.00 \times \sin(30^\circ)}{1.52} = 0.329$$

$$\Rightarrow \theta_2 = \sin^{-1}(0.329) = 19.2^\circ$$



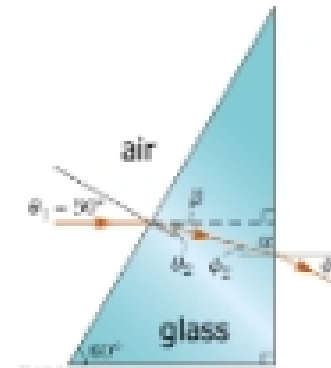
Example $n_2 \sin(\theta_2) = n_1 \sin(\theta_1)$

The index of refraction of this glass is 1.8 for violet light and 1.5 for red light. Calculate the refraction angle θ_1 for both violet and red lights.

(a) Refraction angle θ_1 for violet light

$$\begin{aligned} \sin(\theta_2) &= \frac{n_1 \sin(\theta_1)}{n_2} \\ &= \frac{1.0 \times \sin(30^\circ)}{1.8} \\ &= 0.278 \end{aligned}$$

$$\theta_2 = \sin^{-1}(0.278) = 16.1^\circ$$



Example

Calculate angle θ_1 so that incident angle ϕ_1 is the critical angle at the bottom surface.



Refraction at the $n=1.6/1.4$ interface: $1.6 \times \sin(\theta_1) = 1.4 \times \sin(\theta_2)$

Refraction at the $n=1.4/1.2$ interface: $1.4 \times \sin(\theta_2) = 1.2 \times \sin(\theta_3)$

Refraction at the $n=1.2/1.0$ interface: $1.2 \times \sin(\theta_3) = 1.0 \times \sin(90^\circ)$

Upon observation, we have

$$1.6 \times \sin(\theta_1) = 1.0 \times \sin(90^\circ) = 1$$

$$\theta_1 = \sin^{-1}\left(\frac{1.0}{1.6}\right) = 36.7^\circ$$

b) The energy of photon having wavelength of 740 nm

$$\begin{aligned} E &= \frac{hc}{\lambda} \\ &= \frac{6.626 \times 10^{-34} \times 3 \times 10^8}{740 \times 10^{-9} \times 10^{-9}} \\ E &= 2.686 \times 10^{-19} \text{ J} \end{aligned}$$

In eV

$$\begin{aligned} E &= \frac{2.686 \times 10^{-19}}{1.6 \times 10^{-19}} \\ E &= 1.678 \text{ eV} \end{aligned}$$