

Amortized Complexity

- ✓ Aggregate method.
- Accounting method.
- Potential function method.

Potential Function

- $P(i) = \text{amortizedCost}(i) - \text{actualCost}(i) + P(i - 1)$
- $\Sigma(P(i) - P(i - 1)) =$
 $\Sigma(\text{amortizedCost}(i) - \text{actualCost}(i))$
- $P(n) - P(0) = \Sigma(\text{amortizedCost}(i) - \text{actualCost}(i))$
- $P(n) - P(0) \geq 0$
- When $P(0) = 0$, $P(i)$ is the amount by which the first i operations have been over charged.

Potential Function Example

$a = x + ((a + b) * c + d) + y;$

actual cost 1 1 1 1 1 1 1 1 5 1 1 1 1 7 1 1 7

amortized cost 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2

potential 1 2 3 4 5 6 7 8 9 6 7 8 9 10 5 6 7 2

Potential = stack size except at end.