

# Class 24: Computability



*Halting Problems Hockey Team Logo*



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# Menu

- **Review:**
  - Gödel's Theorem
  - Proof in Axiomatic Systems
- **Computability:**

Are there some problems that it is impossible to write a program to solve?



# Gödel's Proof

$G$ : This statement of number theory does not have any proof in the system of  $PM$ .

If  $G$  were provable, then  $PM$  would be inconsistent.

If  $G$  is unprovable, then  $PM$  would be incomplete.

**$PM$  cannot be complete and consistent!**

