

$$B = \left\langle \frac{1}{\sqrt{2}}, 0, \frac{1}{\sqrt{2}} \right\rangle$$

$$N = B \times T$$

$$B \times T = \begin{vmatrix} i & j & k \\ 1 & 0 & 1 \\ -\sin t & \cos t & \sin t \end{vmatrix} = \frac{1}{\sqrt{2}} \begin{vmatrix} i & j & k \\ 1 & 0 & 1 \\ -\sin t & \cos t & \sin t \end{vmatrix}$$

$$N = \left\langle -\cos t, -2\sin t, \cos t \right\rangle \frac{1}{\sqrt{2} \sqrt{1 + 4\sin^2 t}}$$

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OR solve for N by ...

$$a = \frac{d}{dt} |v| T + |v|^2 \kappa N$$

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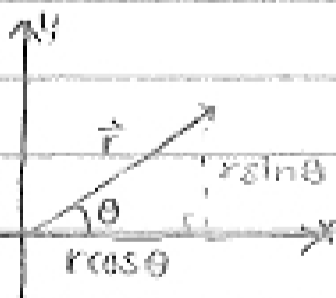
$$N = \frac{a - \frac{d}{dt} |v| T}{|a - \frac{d}{dt} |v| T|}$$

Not good unless speed is constant or easy to take derivative of.

9/8/14

* EXAM over Chapter 13 Friday during class!

Polar Coordinates



Angular momentum (L)

$$\vec{L} = m \vec{r} \times \vec{v}$$

$$\begin{aligned} \frac{d\vec{L}}{dt} &= \frac{d}{dt} m \vec{r} \times \vec{v} \\ &= m \left(\frac{d\vec{r}}{dt} \times \vec{v} + \vec{r} \times \frac{d\vec{v}}{dt} \right) \\ &= m (\vec{v} \times \vec{v} + \vec{r} \times \vec{a}) \\ &= m (\vec{v} \times \vec{v} + \frac{g(r, \theta)}{m} \vec{r} \times \vec{r}) \\ &= \vec{0} \end{aligned}$$



* L is constant

So $\vec{r} \neq \vec{v}$ are always in same plane.

$T = \frac{v(r)}{r^2}$ $N = \frac{dr}{dt} \frac{d\theta}{dt}$ $k = \frac{d^2r}{dt^2}$ $s(t) = \int_0^t |v(t)| dt$

$\vec{U}_\theta = \langle -\sin\theta, \cos\theta \rangle$ $\vec{U}_r = \langle \cos\theta, \sin\theta \rangle$



$\frac{d}{dt} \vec{U}_r = \langle -\sin\theta \frac{d\theta}{dt}, \cos\theta \frac{d\theta}{dt} \rangle$
 $= \frac{d\theta}{dt} \langle -\sin\theta, \cos\theta \rangle$
 $= \frac{d\theta}{dt} \vec{U}_\theta$
 $\frac{d}{dt} \vec{U}_\theta = -\vec{U}_r$

$\vec{v} = \frac{dr}{dt} \vec{U}_r$
 $= \frac{d}{dt} (r \vec{U}_r)$
 $= \frac{dr}{dt} \vec{U}_r + r \frac{d\vec{U}_r}{dt}$
 $= \frac{dr}{dt} \vec{U}_r + r \frac{d\theta}{dt} \vec{U}_\theta$

$\vec{L} = m r \times v$
 $= m r \vec{U}_r \times (\frac{dr}{dt} \vec{U}_r + r \frac{d\theta}{dt} \vec{U}_\theta)$
 $= m r^2 \frac{d\theta}{dt} \vec{U}_r \times \vec{U}_\theta$
 $= m r^2 \frac{d\theta}{dt} \vec{k}$
 * $m r^2 \frac{d\theta}{dt}$ is constant

Conic section



e - eccentricity

$PF = ePD$
 $r = (p + r \cos\theta)e$
 $r - r \cos\theta = ep$
 $r(1 - \cos\theta) = ep$
 $r = \frac{ep}{1 - \cos\theta}$

$\vec{F} = -\frac{mC}{r^2} \vec{U}_r$

(F is origin)