

# Career Services and Fundamental Concepts in Environmental Engineering

CIEG -125 Introduction to Civil  
Engineering

Fall 2005

Lecture 6

## Today

- Career Services
- **Ethics – Groups 10, 11 and 12**
- Fundamental Concepts in Environmental Engineering
- Scheduling the Final Exam

## Fundamental Concepts in Environmental Engineering Outline

- Important Dimensions and Units
  - density
  - concentration
  - flow rate
  - residence time
- Mass balance w/one material

## Density

- Mass divided by unit volume

$$\rho = M/V$$

$$\rho = \text{density (kg/m}^3, \text{lb}_M\text{/ft}^3)$$

M = mass

V = volume

- $\rho_{\text{water}} = 1 \times 10^3 \text{ kg/m}^3 = 1 \text{ g/cm}^3 = 62.4 \text{ lb}_M\text{/ft}^3$

## Concentration

- Gravimetric definition: mass of material A in a unit volume of material consisting of material A and other materials B.

$$C_A = M_A / (V_A + V_B)$$

$C_A$  = concentration of A ( kg/m<sup>3</sup>, mg/L. used in EE)

$M_A$  = mass of material A

$V_A$  = volume of material A

$V_B$  = volume of material B

## Example

Plastic beads with a volume of 0.04 m<sup>3</sup> and a mass of 0.48 kg are placed in a container and 100 L of water are poured into the container.  
What is the concentration of plastic beads in mg/L?

$$\begin{aligned} C_A &= M_A / (V_A + V_B) \\ &= (0.48 \text{ kg}) / (0.04 \text{ m}^3 + 100 \text{ L} (1 \text{ m}^3 / 1000 \text{ L})) \\ &= 3.43 \text{ kg/m}^3 \\ &= 3.43 \text{ kg/m}^3 (10^6 \text{ mg/kg}) / (10^3 \text{ L/m}^3) \\ &= 3430 \text{ mg/L.} \end{aligned}$$

## Example 2

Plastic beads with a volume of  $0.04 \text{ m}^3$  and a mass of  $0.48 \text{ kg}$  are placed in a  $100 \text{ L}$  container into which water is poured filling the container to the brim. What is the concentration of plastic beads in  $\text{mg/L}$ ?

$$\begin{aligned}V_A + V_B &= 100 \text{ L} \\c_A &= M_A / (V_A + V_B) \\&= 0.48 \text{ kg} / 100 \text{ L} \\&= 0.0048 \text{ kg/L} \\&= 0.0048 \text{ kg/L} \cdot (10^6 \text{ mg/kg}) \\&= 4800 \text{ mg/L}\end{aligned}$$

## Concentration: ppm

- Another measure of concentration is ppm or *parts per million*
- If the fluid is water ( $\rho = 1 \text{ g/cm}^3$ ):
$$\begin{aligned}1 \text{ mg/L} &= (0.001 \text{ g})/1000 \text{ mL} \\&= (0.001 \text{ g})/1000 \text{ cm}^3 \\&= (0.001 \text{ g})/1000 \text{ g} \\&= 1 \text{ g} / 10^6 \text{ g} = 1 \text{ ppm}\end{aligned}$$

## Concentration: percentage

- Some material concentrations are expressed as percentages, by mass:

$$\Phi_A = 100 * M_A / (M_A + M_B)$$

- The percentage can also be expressed by volume:

$$\Phi_A = 100 * V_A / (V_A + V_B)$$

## Example

A wastewater sludge has a solids concentration of  $10,000 \text{ ppm}$ . Express this concentration in percent solids (mass basis), assuming that the density of the solids is  $1 \text{ g/cm}^3$ .

$$10,000 \text{ ppm} = 10^4 \text{ g} / 10^6 \text{ g} = 1/100 = 1 \%$$

## Pollution Concentrations in Air

- In air pollution, concentrations are usually expressed in  $\mu\text{g}/\text{m}^3$  of air
- $1 \text{ microgram } (\mu\text{g}) = 10^{-6} \text{ g}$
- Sometimes, concentrations are expressed in terms of ppm, by volume
- Conversion of  $\mu\text{g}/\text{m}^3$  to ppm (Volume/Volume) requires knowledge of the gram molecular weight of the gas

## Moles and GMW of Gases

- 1 mole is made up of  $6.02 \times 10^{23}$  molecules
- 1 mole is the amount of a gas in grams numerically equivalent to its molecular weight
- 1 mole of  $\text{CO}_2$  weighs:
  - $12 + 16 + 16 = 44 \text{ g CO}_2$
  - A.k.a. gram molecular weight (GMW)
- At standard condition ( $0^\circ\text{C}$  and  $1 \text{ atm}$  of pressure), 1 mole of any gas occupies  $22.4 \text{ L}$ .

## Converting $\mu\text{g}/\text{m}^3$ to ppm

ppm (V/V) = (1 m<sup>3</sup> of pollutant / 10<sup>6</sup> m<sup>3</sup> of air)

$$\begin{aligned} X \mu\text{g}/\text{m}^3 &= (X \mu\text{g of pollutant} / 1 \text{ m}^3 \text{ of air}) \\ &= [X \mu\text{g of pollutant} \cdot (1 \text{ g} / 10^6 \mu\text{g}) \cdot (1 \text{ mole} / \text{GMW g}) \cdot \\ &\quad (22.4 \text{ L/mole})] / [1 \text{ m}^3 \text{ of air} \cdot (10^3 / 10^6)] \\ &= [X \mu\text{g of pollutant} \cdot (1 \text{ g} / 10^6 \mu\text{g}) \cdot 10^3 \cdot (1 \text{ mole} / \text{GMW g}) \cdot \\ &\quad (22.4 \times 10^{-3} \text{ m}^3/\text{mole})] / [10^6 \text{ m}^3 \text{ of air}] \\ &= [(X \cdot 22.4 \times 10^{-3} / \text{GMW}) \text{ m}^3 \text{ of pollutant}] / [10^6 \text{ m}^3 \text{ of air}] \\ &= [X \cdot 22.4 \times 10^{-3} / \text{GMW}] \text{ ppm} \\ &= [X \cdot 22.4 / (\text{GMW} \cdot 1000)] \text{ ppm} \end{aligned}$$

## Example: Gaseous Pollution

- If a concentration of 600  $\mu\text{g}/\text{m}^3$  of sulfur dioxide is in air at standard conditions, what is the ppm of this pollutant?

Sulfur dioxide (SO<sub>2</sub>) has one sulfur atom and two oxygen atoms  
 GMW = (32 + 16 + 16) g/mole = 64 g/mole  
 ppm = [(600 · 22.4) / (64 · 1000)] = m<sup>3</sup>/mole  
 = 0.21 ppm

## Flow Rate

- Flow Rate can either be:
  - gravimetric (mass) flow rate (kg/s or lb<sub>M</sub>/s); or
  - volumetric (volume) flow rate (m<sup>3</sup>/s or ft<sup>3</sup>/s)
- dependent quantities because:
 
$$[\text{mass}] = [\text{density}] \times [\text{volume}]$$
- Mass flow rate, Q<sub>M</sub>, is the amount of mass passing a point during a unit of time
- Volume flow rate, Q<sub>V</sub>, would be the volume of that same mass of material passing

## Flow rate, con't

- $Q_M = Q_V \cdot \rho$
- Suppose that we have a volumetric flow of materials A and B, Q<sub>V(A+B)</sub>, and we know the concentration of A, C<sub>A</sub>.
- The mass flow rate of A is:
 
$$Q_{MA} = C_A \cdot Q_{V(A+B)}$$
- This is different from first equation, which is only applicable for one material.

## Example

A wastewater treatment plant discharges a flow of 1.5 m<sup>3</sup>/s (water plus solids) at a solids concentration of 20 mg/L (20 mg of solids per liter of flow, solids plus water). How much solid material is the plant discharging per day?

$$\begin{aligned} Q_{M \text{ SOLIDS}} &= C_{\text{SOLIDS}} \cdot Q_{V(\text{WATER} + \text{SOLIDS})} \\ &= [20 \text{ mg/L} \cdot (10^{-6} \text{ kg/mg})] \cdot [1.5 \text{ m}^3/\text{s} \cdot (10^3 \text{ L/m}^3) \cdot (86,400 \text{ s/day})] \\ &= 2592 \text{ kg/day} \end{aligned}$$

## Example

A drinking water treatment plant adds fluorine at a concentration of 1 mg/L and the average daily demand is 18 million gallons. How many pounds of fluorine must the community purchase?

$$\begin{aligned} Q_{M \text{ FLUORINE}} &= C_{\text{FLUORINE}} \cdot Q_{V(\text{WATER})} \\ &= (1 \text{ mg/L}) \cdot (3.79 \text{ L/gal}) \cdot (2.2 \times 10^6 \text{ ft}^3/\text{mg}) \cdot (18 \times 10^6 \text{ gal/day}) \\ &= 150 \text{ lbs/day} \end{aligned}$$