

This exam should have 18 questions. Part I will have 16 multiple choice questions, 5 points each. Part II will have 2 handgraded questions, 10 points each. Please check to see that your exam is complete. If you do not have a **PENCIL** to mark your card, please ask to borrow one from your proctor.

Write your **ID NUMBER** (not your SS number) on the six blank lines on the top of your answer card, using one blank for each digit. **Shade in the corresponding boxes below**. Also **Print your name at the top of your card**.

**PART I** : ( 80 points )

1) Find the sum of the series,  $\frac{4}{9} + \frac{4}{27} + \frac{4}{81} + \frac{4}{243} + \dots$ , if it converges.

- A)  $\frac{5}{9}$
- B)  $\frac{10}{9}$
- C)  $\frac{10}{9}$
- D)  $\frac{10}{9}$
- E)  $\frac{10}{9}$
- F)  $\frac{10}{9}$
- G)  $\frac{10}{9}$
- H)  $\frac{10}{9}$
- I)  $\frac{10}{9}$
- J) *diverges*

2) Find the **limit** of the sequence  $\left\{ \frac{1}{(1/10)^n} \right\}_{n=1}^{\infty}$ , if it converges.

- A) 0
- B) 1
- C)  $\frac{10}{9}$
- D)  $\frac{100}{9}$
- E)  $\frac{211}{9}$
- F) 200
- G)  $\frac{1}{9}$
- H)  $\frac{1}{27}$
- I)  $\frac{1}{81}$
- J) *diverges*

3) Determine whether the sequence  $\left\{ \cos\left(\frac{1}{n}\right) + n \cdot \sin\left(\frac{1}{n}\right) \right\}_{n=1}^{\infty}$  converges or diverges . If it converges then find the limit .

- A)  $\frac{2}{3}$
- B)  $\frac{1}{2}$
- C) 3
- D) 4
- E)  $\frac{2}{5}$
- F) 2
- G) 0
- H)  $\frac{3}{5}$
- I) 1
- J) diverges

4) Find the **sum** of the series  $\sum_{n=1}^{\infty} \frac{1+2^n}{3^n}$  , if it converges .

- A) 1
- B) 1.5
- C) 2
- D) 2.5
- E) 3
- F) 3.5
- G) 4
- H) 4.5
- I) 5
- J) diverges

5) Which of the following three series is **convergent** ?

$$I) \sum_{n=1}^{\infty} \frac{n+2}{n^{3/2}} \quad II) \sum_{n=2}^{\infty} \frac{1}{n \cdot \ln(n)} \quad III) \sum_{n=1}^{\infty} \frac{n}{\sqrt{1+n^2}}$$

A) I B) II C) III D) I & II E) I & III F) II & III G) I, II & III H) all diverge

6) If  $s = \sum_{n=1}^{\infty} \frac{1}{n^3}$  and  $s_{10} = \sum_{n=1}^{10} \frac{1}{n^3}$  (10<sup>th</sup> partial sum) then from **bounds for the remainder in the integral test**, we know that  $|s - s_{10}|$  is less than :

- A) 0.01
- B) 0.001
- C) 0.002
- D) 0.03
- E) 0.004
- F) 0.05
- G) 0.005
- H) 0.06
- I) 0.007
- J) 0.07