

1. (a) False. This would be true for  $e^{x+y}$ .  
 (b) True.  
 (c) True  
 (d) True. When using the values of  $\theta$ , the only requirement is that the starting value and ending value can not have a difference of more than  $2\pi$ .  
 (e) False. To be true the inside integral needs to start at  $z = 0$  not  $z = 1$ .
2. (a)  $x^2 + y^2 = 4y$  this is a circle.  
 (b)  $\rho = 2 \sec(\phi)$   
 $\rho \cos \phi = 2$   
 $z = 2$  this is a plane

3. Note: Since  $f(x, y)$  is not a constant function, the volume of each of the 5 solids formed with the base being the leaf and the height being  $f(x, y)$  will not be equal.

Note 2: you can not integrate from 0 to  $2\pi$  since on parts of this interval the radius will be negative.

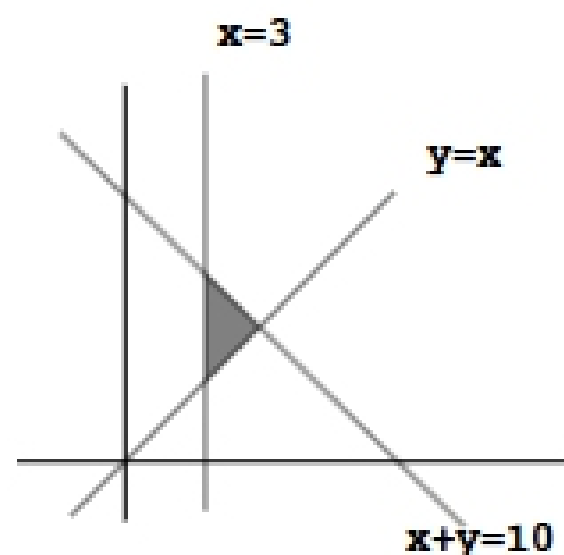
I have set up the integral for the leaf that is centered on the positive x-axis.

$$\int_{-\pi/10}^{\pi/10} \int_0^{\cos(5\theta)} 3r^3 \sin^2 \theta \, dr d\theta$$

4. Change the limits of the integral to get:  $\int_0^2 \int_0^{2y} e^{y^2} \, dx dy$ .

integrating this gives  $e^4 - 1$

5. The correct region has been shaded in the graph.



$$\int_3^5 \int_x^{10-x} \sqrt{4^2 + 2^2 + 1} \, dy dx = \dots = 4\sqrt{21}$$

6. The surface is given by  $z = \sqrt{9 - y^2}$  so we get  $z_x = 0$  and  $z_y = \frac{-y}{\sqrt{9 - y^2}}$

$$\int_0^2 \int_0^{\sqrt{4-x^2}} \sqrt{\frac{y^2}{9-y^2} + 1} \, dy dx = \int_0^2 \int_0^{\sqrt{4-x^2}} \sqrt{\frac{9}{9-y^2}} \, dy dx$$

$$\text{or } \int_0^{\pi/2} \int_0^2 r \sqrt{\frac{9}{9-r^2 \sin^2 \theta}} \, dr d\theta$$

7. Step 1 find the intersection of the sphere and the paraboloid.

The paraboloid gives  $z+4 = x^2+y^2$  substituting this into the sphere equation gives  $z+4+z^2 = 6$ . Solving gives  $z = 1$  and  $z = -2$ . Since this is the top of the sphere  $z = 1$  is what we want.

The intersection is  $x^2 + y^2 + (1)^2 = 6$  or  $x^2 + y^2 = 5$

Also note that  $y \geq 0$  means that  $0 \leq \theta \leq \pi$ .

$$\int_0^\pi \int_0^{\sqrt{5}} \int_{r^2-4}^{\sqrt{6-r^2}} r \, dzdrd\theta$$

$$8. \int_0^3 \int_0^{12-4y} \int_y^{(12-2y-z)/2} f(x, y, z) \, dx dz dy$$

$$9. \text{ (a) } \int_{-\pi/2}^{\pi/2} \int_0^5 \int_r^{\sqrt{50-r^2}} zr^2 \sin \theta \, dzdrd\theta$$

$$\text{ (b) } \int_{-\pi/2}^{\pi/2} \int_0^{\pi/4} \int_0^{\sqrt{50}} \rho^4 \sin^2 \phi \cos \phi \sin \theta \, d\rho d\phi d\theta$$

$$10. \int_0^{2\pi} \int_3^6 \int_1^{r \sin \theta + 40} r^2 \cos \theta \, dzdrd\theta$$

$$11. \int_{-2}^2 \int_{y^2}^{8-y^2} k((x-14)^2 + y^2) \, dx dy$$