

## Chapter 5 – MOLECULAR SPECTROSCOPY



## The Schrödinger equation for $H_2^+$

$$\left( \mathbf{T}_{\text{nuc}} + \mathbf{H}_{\text{el}} + \frac{e^2}{R} \right) \Psi(\vec{\mathbf{R}}, \vec{\mathbf{r}}) = E \Psi(\vec{\mathbf{R}}, \vec{\mathbf{r}})$$

When the Born-Oppenheimer approximation is applied, the electronic motion can be separated from the nuclear motion;

$$\left[ \mathbf{H}_{\text{el}} + \frac{e^2}{R} \right] \psi_{\text{el}}(\mathbf{R}, \vec{\mathbf{r}}) = E(\mathbf{R}) \psi_{\text{el}}(\mathbf{R}, \vec{\mathbf{r}})$$

where

$$\mathbf{H}_{\text{el}} = -\frac{\hbar^2}{2m} \nabla_{\vec{\mathbf{r}}}^2 - e^2 \left( \frac{1}{r_{\text{Ae}}} + \frac{1}{r_{\text{Be}}} \right)$$

Once  $\psi_{\text{el}}$  and  $E(\mathbf{R})$  have been determined as a function of  $\mathbf{R}$ , the nuclear motion may be treated;

$$\left[ \mathbf{T}_{\text{nuc}} + E(\mathbf{R}) \right] \psi_{\text{nuc}}(\vec{\mathbf{R}}) = E \psi_{\text{nuc}}(\vec{\mathbf{R}})$$

## Transitions in molecules

$$\bar{\nu} = \frac{1}{\lambda} = \frac{\nu}{c}$$

**1 wavenumber = 1 cm<sup>-1</sup>**

**Electronic:**       $\Delta E \sim 5 \text{ eV}$   
                          $\lambda \sim 250 \text{ nm}$   
                          $\bar{\nu} \sim 40,000 \text{ cm}^{-1}$

**UV-visible**

**Vibrational:**     $\Delta E \sim 0.2 \text{ eV}$   
                          $\lambda \sim 6.2 \mu\text{m}$   
                          $\bar{\nu} \sim 1600 \text{ cm}^{-1}$

**Infra-red**

**Rotational:**       $\Delta E \sim 4 \times 10^{-4} \text{ eV}$   
                          $\lambda \sim 3 \text{ mm}$   
                          $\bar{\nu} \sim 3 \text{ cm}^{-1}$

**Microwave**