

VI-1

Unknown Resistor	l1 (cm)	l2 (cm)	σ_l (cm)	R3 (Ω)	Rm (DMM) (Ω)
A	50	50	0.05	149	148.78
B	50	50	0.05	215	213
C	50	50	0.05	385	383
D	50	50	0.05	981	982

To calculate Rx and its uncertainty, we use the formula:

$$R_x = R_3(l_2/l_1)$$

$$R_x = R_3(50\text{cm}/50\text{cm})$$

$$\mathbf{R_x = R_3.}$$

$$\sigma_{R_x} = R_3 \left(\frac{1}{l_1} + \frac{l_2}{l_1^2} \right) \sigma_l = R_3 \left(\frac{1}{50} + \frac{50}{50^2} \right) * 0.05 = R_3(0.002)$$

For resistor A, $R_x = R_3 = 149\Omega$ and $\sigma_{R_x} = R_3(0.002) = 149 * 0.002 = 0.298\Omega$

$$R_x \pm \sigma_{R_x} = 149 \pm 0.3\Omega$$

$$R_m = 148.78\Omega$$

For resistor B, $R_x = R_3 = 215\Omega$ and $\sigma_{R_x} = R_3(0.002) = 215 * 0.002 = 0.43\Omega$

$$R_x \pm \sigma_{R_x} = 215 \pm 0.4\Omega$$

$$R_m = 213\Omega$$

For resistor C, $R_x = R_3 = 385\Omega$ and $\sigma_{R_x} = R_3(0.002) = 385 * 0.002 = 0.77\Omega$

$$R_x \pm \sigma_{R_x} = 385 \pm 0.8\Omega$$

$$R_m = 383\Omega$$

For resistor D, $R_x = R_3 = 981\Omega$ and $\sigma_{R_x} = R_3(0.002) = 981 * 0.002 = 1.962\Omega$

$$R_x \pm \sigma_{R_x} = 980 \pm 2\Omega$$

$$R_m = 982\Omega$$

As we can see, for each resistor, A, B, C, D, R_m and $R_x \pm \sigma_R$ lie almost in the same range. There is a slight discrepancy in the values, which causes R_m and $R_x \pm \sigma_R$ to be different by 1 or 2 Ω . This is because of manual errors during measurement. Also, another reason for discrepancies is because we considered the resistance of the Wheatstone bridge wire to be zero, but in reality that wire has some resistance. The lengths are not 100% accurate because we used a ruler to measure the lengths. Since it is not digital, it is accurate only up to 1mm. The least calibration on the ruler is 1mm and therefore, we assumed σ_l to be 1mm/2, that is, 0.5mm. This could be another reason for the discrepancy in the resistances.

VI-2

Unknown Resistor	l1 (cm)	l2 (cm)	σ_l (cm)	R3 (Ω)	Rm (DMM) (Ω)
A	50	50	0.05	147	148.78
B	50	50	0.05	214	213
C	50	50	0.05	380	383
D	50	50	0.05	980	982

To calculate R_x and its uncertainty, we use the formula:

$$R_x = R_3(l_2/l_1)$$

$$R_x = R_3(50\text{cm}/50\text{cm})$$

$$\mathbf{R_x = R_3.}$$

$$\sigma_R = R_3 \left(\frac{1}{l_1} + \frac{l_2}{l_1^2} \right) \sigma_l = R_3 \left(\frac{1}{50} + \frac{50}{50^2} \right) * 0.05 = R_3(0.002)$$

For resistor A, $R_x = R_3 = 147\Omega$ and $\sigma_R = R_3(0.002) = 147 * 0.002 = 0.294\Omega$

$$R_x \pm \sigma_R = 147 \pm 0.3\Omega$$

$$R_m = 148.78\Omega$$

For resistor B, $R_x = R_3 = 214\Omega$ and $\sigma_R = R_3(0.002) = 214 * 0.002 = 0.428\Omega$

$$R_x \pm \sigma_R = 214 \pm 0.4\Omega$$

$$R_m = 213\Omega$$

For resistor C, $R_x = R_3 = 380\Omega$ and $\sigma_{R_x} = R_3(0.002) = 380 * 0.002 = 0.76\Omega$
 $R_x \pm \sigma_{R_x} = 380 \pm 0.8\Omega$

$$R_m = 383\Omega$$

For resistor D, $R_x = R_3 = 980\Omega$ and $\sigma_{R_x} = R_3(0.002) = 980 * 0.002 = 1.96\Omega$
 $R_x \pm \sigma_{R_x} = 980 \pm 2\Omega$

$$R_m = 982\Omega$$

Just like, VI-1, for each resistor, A, B, C, D, R_m and $R_x \pm \sigma_{R_x}$ lie almost in the same range. There is a slight discrepancy in the values, which causes R_m and $R_x \pm \sigma_{R_x}$ to be different by 1 or 2 Ω . This is because of manual errors during measurement. Also, another reason for discrepancies is because we considered the resistance of the Wheatstone bridge wire to be zero, but in reality that wire has some resistance. The lengths are not 100% accurate because we used a ruler to measure the lengths. Since it is not digital, it is accurate only up to 1mm. The least calibration on the ruler is 1mm and therefore, we assumed σ_l to be 1mm/2, that is, 0.5mm. This could be another reason for the discrepancy in the resistances.

Comparison table between DC and AC values:

Unknown Resistor	$R_x \pm \sigma_{R_x}, \Omega$ For DC	$R_x \pm \sigma_{R_x}, \Omega$ for AC
A	$149 \pm 0.3\Omega$	$147 \pm 0.3\Omega$
B	$215 \pm 0.4\Omega$	$214 \pm 0.4\Omega$
C	$385 \pm 0.8\Omega$	$380 \pm 0.8\Omega$
D	$980 \pm 2\Omega$	$980 \pm 2\Omega$

Clearly, the uncertainties for R_x , that is σ_{R_x} for both DC and AC values is the same. The R_x for both DC and AC is almost similar.