

1) Cojoe Couriers has perpetual EBIT of \$4 million per year. The all-equity discount rate  $R_0$  for Cojoe Couriers is 15 percent. The company's tax rate is 35 percent. The cost of debt capital is 10 percent, and the company has \$10 million of debt in its capital structure.

- What is Cojoe Courier's firm value?
- What is Cojoe Courier's cost of equity ( $R_S$ )?
- What is Cojoe Courier's  $R_{WACC}$ ?

**Ans.**

Here, it is given that

EBIT = \$4 million Per year (perpetuity)

$R_0 = 15\%$ , Tax rate  $T_c = 35\%$ ,  $R_B = 10\%$ ,  $B = \$10$  million

$$a) V_L = V_U + (B * T_c)$$

$$\begin{aligned} V_U &= \text{EBIT} * (1 - T_c) / R_0 \\ &= \$4 \text{ million} * (1 - .35) / .15 \\ &= \$17.3 \text{ million} \end{aligned}$$

$$\begin{aligned} \text{So, } V_L &= \$17.3 \text{ million} + (\$10 \text{ million} * .35) \\ &= \$20.8 \text{ million} \end{aligned}$$

$$\begin{aligned} b) R_S &= R_0 + (R_0 - R_B) * (B/S) * (1 - T_c) \\ \text{As, } V_L &= B + S \\ S &= \$10.8 \text{ million} \\ R_S &= .15 + (.15 - .10) * (10/10.8) * (1 - .35) \\ &= .18 \text{ or } 18\% \end{aligned}$$

$$\begin{aligned} c) R_{WACC} &= R_S * (S/V) + R_B * (B/V) * (1 - T_c) \\ &= .18 * (10.8/20.8) + 0.10 * (10/20.8) * (1 - .35) \\ &= 0.12 \text{ or } 12\% \end{aligned}$$

2) A.J. Electronics currently has 700,000 shares of stock outstanding. The total firm value of A.J. is \$3 million and it has \$750,000 of debt. This debt is a perpetuity. The company is in the 34% tax bracket. If A.J. were fully unlevered, the equity holders would require a 15% return (i.e.,  $R_0 = 15\%$ ). The cost of borrowing is 10%.

- What is the required rate of return on equity for A.J.'s shareholders?
- What is A.J.'s WACC?
- What would the value of the firm be had it been financed entirely with equity?

d) What would the value of the firm be had it been financed with \$1 million debt instead?

**Ans.**

Here, it is given that

$$V_L = \$3 \text{ million}$$

$$R_0 = 15\%, \text{ Tax rate } T_c = 34\%, R_B = 10\%, B = \$ .75 \text{ million}$$

- a)  $R_S = R_0 + (R_0 - R_B) (B/S) (1 - T_c)$   
 As,  $V_L = B + S$   
 $S = \$2.25 \text{ million}$   
 $R_S = .15 + (.15 - .10) * (.75/2.25) * (1-.34)$   
 $= .16 \text{ or } 16\%$
- b)  $R_{WACC} = R_S * (S/V) + R_B * (B/V) * (1 - T_c)$   
 $= .16 * (2.25/3) + 0.10 * (.75/3) * (1-.34)$   
 $= 0.14 \text{ or } 14\%$
- c) Had the firm been financed entirely with equity , its value be  
 $V_U = S = \$2.25 \text{ million}$
- d) As,  $V_L = B + S$  and  $B = \$1 \text{ million}$   
 $V_L = 1 + 2.25 = \$3.25 \text{ million}$

3) Multicare Corporation an all-equity firm has perpetual EBIT of \$2.5 million per year. The all- equity discount rate  $R_0$  is 20%. The company's tax rate is 34%. Although the firm does not have any debt now, if it decides to borrow then it's (before-tax) cost of debt capital would be 12%.

- a) What is Multicare's firm value now?  
 b) What is Multicare's  $R_{WACC}$  if it decides to use debt financing to cover 30% of its firm value?  
 c) What is Multicare's cost of equity ( $R_S$ ), if the firm issues \$5 mil. of debt and repurchases \$5 mil. of equity, i.e., Multicare simply alters its capital structure without altering its business operations or its EBIT. Assume that the debt is a perpetuity.

{Note that in part (c) the change in capital structure alters the firm value.}

**Ans.**

Here it is given that EBIT = \$2.5 million per year (perpetuity)

$$R_0 = 20\%, T_c = 34\%$$

a)

$$\text{Firm value } V_L = V_U + (B * T_c)$$

$$\text{Since } B = 0, V_L = V_U$$

$$V_U = \text{EBIT} * (1-T_c)/R_0$$

$$= \$2.5 \text{ million} * (1-.34) / 0.2$$

$$= \$8.25 \text{ million} = V_L$$

$$\text{b) Now, } B = 0.3 * V_L = \$2.475 \text{ million}$$

$$\text{And } S = V_L - B = \$5.775 \text{ million}$$

$$R_B = 12\% \text{ given}$$

We need to first find out  $R_S$

$$\begin{aligned} R_S &= R_0 + (R_0 - R_B) * (B/S) * (1 - T_c) \\ &= 0.2 + (0.2 - 0.12) * (2.475/5.775) * (1 - 0.34) \\ &= 0.2226 \text{ or } 22.26\% \end{aligned}$$

$$\begin{aligned} \text{Now, } R_{WACC} &= R_S * (S/V) + R_B * (B/V) * (1 - T_c) \\ &= .2226 * (5.775/8.25) + .12 * (2.475/8.25) * (1 - .34) \\ &= 0.1796 \text{ or } 17.96\% \end{aligned}$$

$$\text{c) } R_S = R_0 + (R_0 - R_B) (B/S) (1 - T_c)$$

$$B = 5 \text{ million}$$

The firm now has 5 million of debt. So the firm value is higher than in part (a) due to the debt tax shields.

$$\begin{aligned} V_L &= V_U + B * T_c \\ &= 8.25 \text{ million} + 5 \text{ million} * (0.34) \\ &= 9.95 \text{ million} \end{aligned}$$

So now,  $S = 9.95 - 5 = 4.95$  million and

$$\begin{aligned} R_S &= (0.2) + (0.2 - 0.12) * (5/4.95) * (1 - 0.34) \\ &= \mathbf{0.2533} \end{aligned}$$

- 4) Zack's Inc., an all-equity firm, is subject to a 30% corporate tax rate. Its equity holders require a 20% return. The firm's market value now is \$3,500,000, and there are 175,000 shares outstanding. Suppose the firm issues \$1 million of bonds at 10% and uses the proceeds to repurchase common stock. What is the market value of equity of the firm after the debt issue?

**Ans.**

$$V_L = V_U = \$3.5 \text{ million}$$

$$T_c = 30\%$$

$$\text{Now, } B = \$1 \text{ million}$$

$$\begin{aligned} \text{So, } V_L &= V_U + B * T_c \\ &= 3.5 + 1 * 0.30 \\ &= \$3.8 \text{ million} \end{aligned}$$

$$\text{So, } S \text{ (Market value of Equity)} = 3.8 - 1 = \$2.8 \text{ million}$$

- 5) Weston Industries has a debt–equity ratio of 1.5. Its WACC is 11 percent, and its cost of debt is 7 percent. The corporate tax rate is 35 percent.
- What is Weston's cost of equity capital?
  - What is Weston's unlevered cost of equity capital?
  - What would the cost of equity be if the debt–equity ratio were 2? What if it were 1.0? What if it were zero?