

Chi-Squared Goodness-of-Fit Test -

- Multinomial Experiment
 - o Consists of a fixed number of n trials
 - o The outcome of each trial can be classified into one of k categories, called *cells*
 - o The probability p that the outcome will fall into cell i remains constant for each trial
 - o Each trial of the experiment is independent of other trials
- Hypotheses:
 - o $H_0: p_1 = \#, p_2 = \#, p_3 = \#$ etc.
 - o $H_A: \text{At least one } p_i \text{ is not equal to its specified value}$
- Expected value: $e_i = np_i$
- $\chi^2 = \sum (f_i - e_i)^2 / e_i$

Make a table:

| Category | Observed frequency | Expected frequency | (f - e) | (f - e) ² / e |
|----------|--------------------|--------------------|---------|--------------------------|
| A | | | | |
| B | | | | |
| Total | | | | $\chi^2 = \#$ |

Rejection Region: $\chi^2 > \chi^2_{\alpha, k-1}$

- Describes a single population
- Nominal data
- 2 or more categories

Chi-Squared Test of a Contingency Table -

EXAMPLE:

$P(\text{Accounting}) = 61/152 = .401$
 $P(\text{Finance}) = 44/152 = .289$
 $P(\text{Marketing}) = 47/152 = .309$

$P(\text{BA}) = 60/152 = .395$
 $P(\text{BEng}) = 31/152 = .204$
 $P(\text{BBA}) = 39/152 = .257$
 $P(\text{Other}) = 22/152 = .145$

| Undergrad Degree | Accounting | Finance | Marketing | Total |
|------------------|--|--|--|-------|
| B.A. | $152 \times 60/152 \times 61/152$ = 24.08 | $152 \times 60/152 \times 44/152$ = 17.37 | $152 \times 60/152 \times 47/152$ = 18.55 | 60 |
| B.Eng. | $152 \times 31/152 \times 61/152$ = 12.44 | | | 31 |
| B.B.A | | | | 39 |
| Other | | | | 22 |
| Total | | | | 152 |

Expected Frequencies = Row total x column total / sample size
 $\chi^2 = (31 - 24.08)^2/24.08 + \dots$

Rejection Region: $\chi^2 > \chi^2_{\alpha, v}$ $v = (r-1)(c-1)$

- Analyzes relationship between two variables and compares two or more opulations
- Nominal data