

Name \_\_\_\_\_

Group Members:

1. For each function, determine the long run behavior, determine the intercepts of the graph of the function, and sketch a rough graph of the function. If applicable, find the vertex of the function.

(a)  $g(x) = -x^2 - 4x - 3$

(b)  $h(x) = x^3 - 4x^2 - 16x + 64$

(c)  $\sigma(x) = x(x + 3)(x + 5) - 10(x + 5)$

2. Show that  $x = \frac{1}{2}$  and  $x = 4$  are solutions of the equation  $0 = 2x^4 - 3x^3 - 19x^2 - 6x + 8$ . Use the result to list all the real solutions of the equation.

3. Juan owns a small business that manufactures knock-off tamagotchis called jamagotchis. His hourly production costs are  $C(x) = 0.5x^2 - 20x + 460$  where  $C$  is the total cost in dollars and  $x$  is the number of toys produced. How many jamagotchis should be produced each hour to yield a minimum cost to Juan's business?

4. Find two positive real numbers whose product is maximum and whose sum is 110.

5. Find the real zeros of the following polynomials

(a)  $f(x) = 2x^3 - 11x^2 + 4x + 5$

(b)  $q(x) = x^4 - x^3 + x^2 - 3x - 6$

(c)  $p(x) = x^4 - 4x^2 + 4$

(d)  $v(x) = (x^2 - 7)^2 - 3(x^2 - 7) + 2$

6. Perform the following polynomial divisions, giving your answer in the form  $f(x) = g(x)q(x) + r(x)$ , where  $q(x)$  is the quotient and  $r(x)$  is the remainder.

(a)  $f(x) \div g(x)$  where  $f(x) = 12x^3 + 4x^2 - x + 5$  and  $g(x) = 3x - 5$

(b)  $f(x) \div g(x)$  where  $f(x) = x^5 + 3x^3 + x^2 + 2x + 2$  and  $g(x) = x^2 + 2$

(c)  $f(x) \div g(x)$  where  $f(x) = -x^3 - x^2 - 8$  and  $g(x) = x - 2$

7. Find a polynomial with integer coefficients with the zeros indicated.

(a)  $0, 5, -9$

(b)  $1, -4, 2$

(c)  $4, \pm\sqrt{5}$

(d)  $3\sqrt{2}, 4$

8. For each function, determine the long run behavior, determine the intercepts of the graph of the function, and sketch a rough graph of the function.

(a)  $g(x) = x^4 + 6x^3 + 10x^2 + 6x + 9$

(b)  $f(x) = x^3 - 13x - 12$

(c)  $h(x) = -3x^2 + 8x$

9. Find the rational zeros of the polynomial  $p(x) = x^3 + x + 1$ .

10. Find the intersection points of the graphs of the functions  $f(x) = \frac{x^2}{3}$  and  $g(x) = 2x - 4$ .

**Challenge:** In question 3, for what price does Juan need to sell each toy in order to break even?