

*Owen Graduate School of Management
Vanderbilt University
Sample Exam*

Game Theory & Business Strategy MGT 425

FINAL EXAMINATION

WRITE YOUR NAME ON THE **BACK** OF THIS EXAM ONLY

This final exam is worth 60 points.

There are 6 questions, each worth 10 points.

On the last page, you may answer any of the questions for a little extra credit.

Please identify any assumptions you are using in your analysis and show all work for partial credit. You may use the back of a page if necessary, but clearly indicate if you do so I will know to look there.

Most Importantly, Have Fun!

QUESTION 1.

Find all pure-strategy Nash equilibria for the following game.

		Mindy		
		X	Y	Z
Mork	A	10 , 30	0 , 20	20 , 30
	B	15 , 35	10 , 40	10 , 40
	C	25 , 25	5 , 25	5 , 25

QUESTION 2.

Consider the game below between Vizzini and Roberts. Each has two strategies. Vizzini's payoffs are given first (in italics). The game has a unique equilibrium.

		Roberts	
		Drink	Pass
Vizzini	<i>Safe</i>	<i>-3</i> , 3	3 , <i>-3</i>
	<i>Risky</i>	3 , <i>-3</i>	<i>-3</i> , 3

A. In equilibrium, what is Vizzini's expected payoff?

Recently, the rules of the game have changed. If Vizzini selects "Safe" and Roberts selects "Pass," the payoffs become (6,-6) instead of (3,-3). All other payoffs remain the same.

B. In equilibrium, is Vizzini *more or less likely to use "Safe"* now with (6,-6) than before with (3,-3)? Explain.

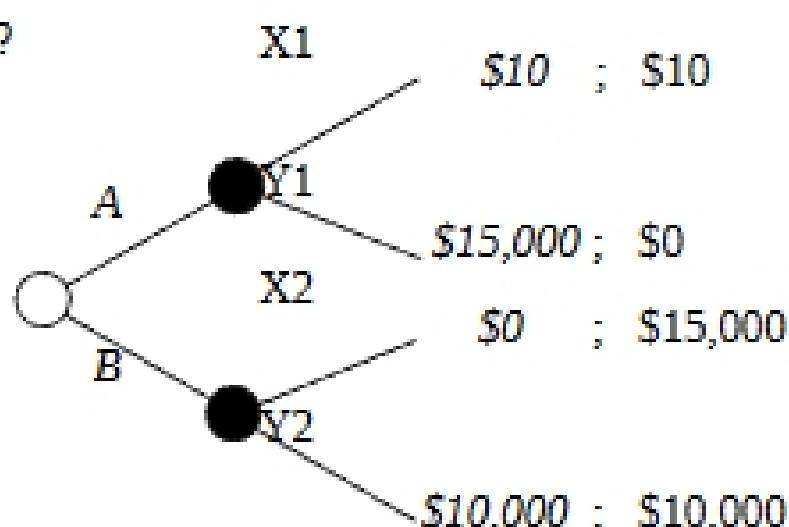
C. In equilibrium, is Roberts *more or less likely to use "Pass"* than before? Explain.

QUESTION 3.

What is the rollback equilibrium of this game?

Player 1 is indicated by a hollow circle and player 2 by a solid circle.

Player 1's payoffs are listed first.



QUESTION 4.

You have invented SnoreMore, a new pill which increases both the frequency and volume of snoring. If your product launch is successful, you can take over the \$600,000 market currently controlled by Date-Be-Gone-Spray. An unsuccessful launch results in profits of \$0. You consider hiring an advertising agency. The agency can either work hard or "soft" on your account. Hard work requires the agency to invest \$400,000 in resources, and soft work requires an investment of \$200,000. Hard work results in a $\frac{3}{4}$ chance of success and soft work results in a $\frac{1}{2}$ chance.

You can only observe the success or failure of the project. The advertising agency is risk-neutral. What is the optimal combination of base salary and bonus to offer the agency?

Assume that the base salary cannot be negative.

Summary: Value = \$600K if successful and \$0 if not
 Hard work: costs \$400K $\frac{3}{4}$ chance of success
 Soft work: costs \$200K $\frac{1}{2}$ chance of success