

EE 503

Lecture # 20

1 November 2016

Midterm #2 - posting -

covers up to and including CLT
and Poisson approximation to Binomial
up to and including lecture 19 page 9.

Advance Reading Ch. 6 Vector RVs

6.3.3 only a little

OMIT 6.3.4

6.6

Read App. C - Matrices + Linear Algebra

From Example 2

$$\underline{P(|X-m| \geq 2\sigma) \leq \frac{1}{4} = 0.25 \text{ in general}}$$

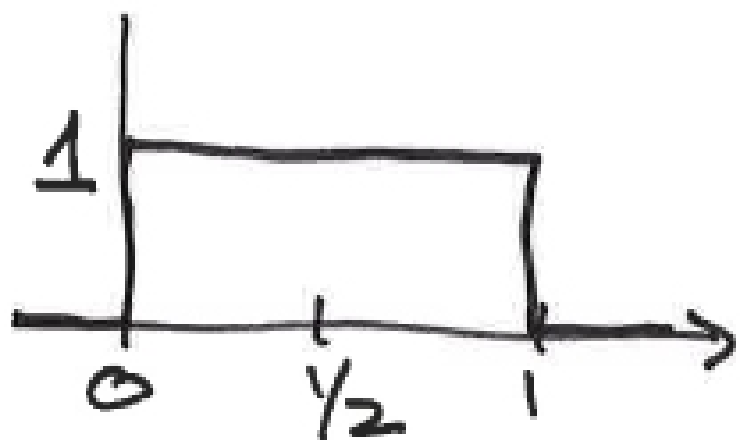
Suppose X is a uniform $[0, 1]$ RV

$$m = \frac{1}{2} \quad \sigma = \frac{1}{2\sqrt{3}} = 0.289$$

$$2\sigma = 0.577$$

$$P(|X-m| \geq 2\sigma) = P\left(|X - \frac{1}{2}| \geq \frac{1}{\sqrt{3}}\right)$$

$$= P(|X - \frac{1}{2}| \geq 0.577) = \underline{\underline{0}}$$



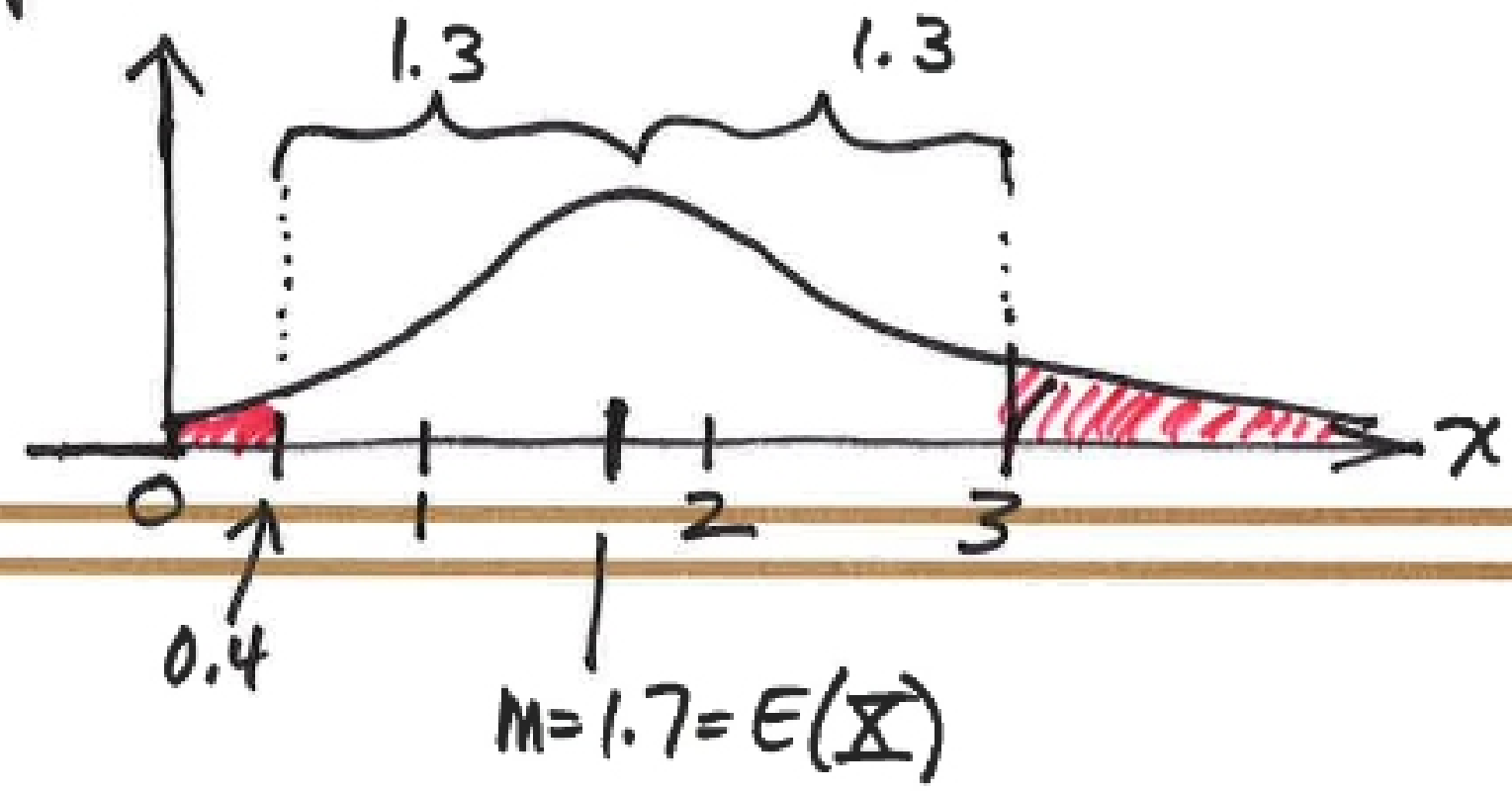
Chebyshev is most useful for smooth, unimodal pdfs.

Note if $\sigma_X = 0$ $P(|X-m| \geq t) = 0$ for all t
so $P(X=m) = 1$

Revisit the EE 503 student height problem $E(X) = 1.7$ add: $\sigma_X = 0.3$

find $P(X > 3)$ start with Chebyshev

$$P(|X - 1.7| \geq 1.3) \leq \left(\frac{0.3}{1.3}\right)^2 = 0.0533$$



$$P(X \leq 0.4) + P(X \geq 3) \leq 0.0533$$

$$P(X \geq 3) \leq 0.0533 - P(X < 0.4)$$

we don't have this, assume the worst case:

$$P(X \geq 3) \leq 0.0533 \quad P(X < 0.4) = 0$$

⇒ from Chebyshev

$$P(X > 3) \leq 0.57 \text{ (Markov)}$$