

## 5.7 - Chebyshev Multi-section Matching Transformer

**Reading Assignment: pp. 250-255**

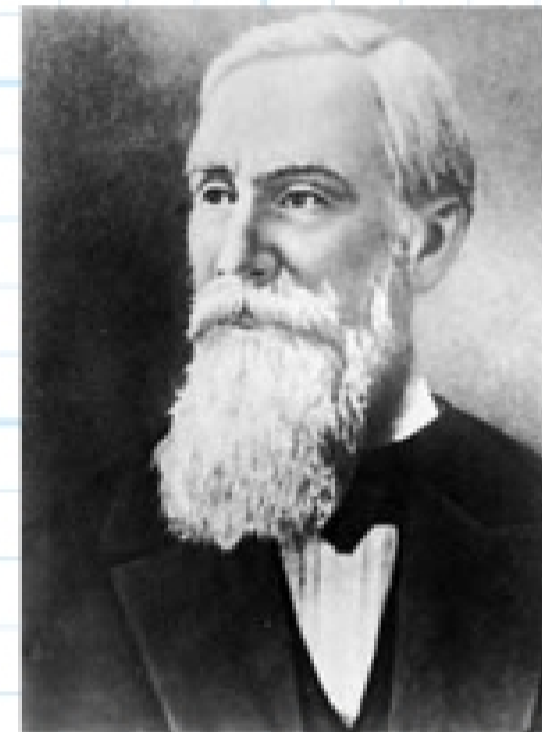
We can also build a multisection matching network such that the function  $\Gamma(f)$  is a **Chebyshev** function.

Chebyshev functions **maximize bandwidth**, albeit at the cost of **pass-band ripple**.

**HO: The Chebyshev Multi-section Matching Transformer**

# The Chebyshev Matching Transformer

An **alternative** to Binomial (Maximally Flat) functions (and there are **many** such alternatives!) are **Chebyshev** polynomials.



**Pafnuty  
Chebyshev**

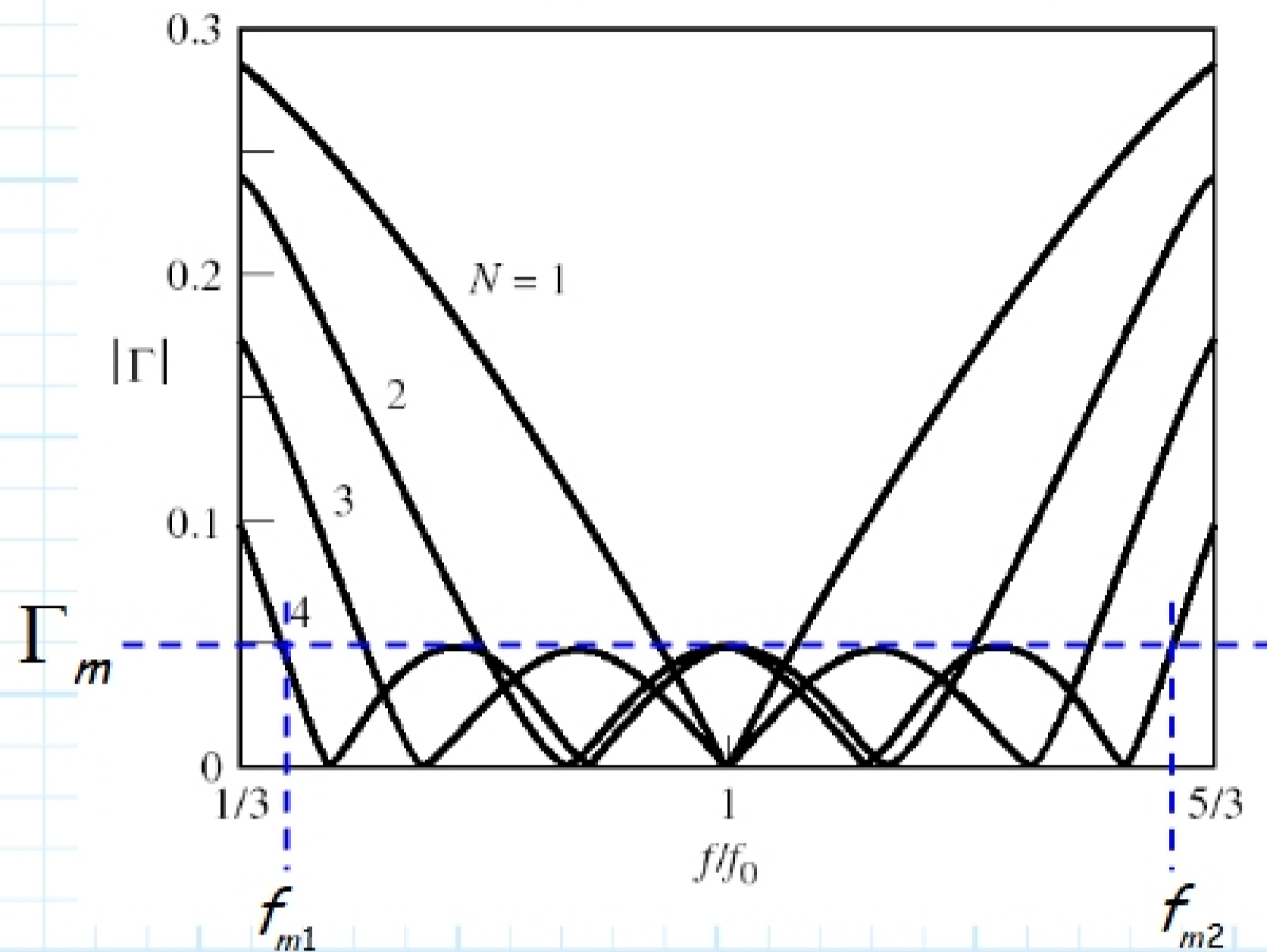
1821 -1894

Chebyshev solutions can provide functions  $\Gamma(\omega)$  with **wider bandwidth** than the Binomial case—albeit at the “expense” of **passband ripple**.

It is evident from the plot below that the Chebyshev response is **far** from maximally **flat**! Instead, a Chebyshev matching network exhibits a “**ripple**” in its passband. Note the magnitude of this ripple never **exceeds** some **maximum** value  $\Gamma_m$  (within the **pass-band**).

The two frequencies at which the value  $|\Gamma(\omega)|$  **does** increase beyond  $\Gamma_m$  define the **bandwidth** of the matching network.

We denote these frequencies  $\omega_m = 2\pi f_m$  (the plot above shows the locations of the frequencies for  $N=4$ ).



**Figure 5.17 (p. 255)**

*Reflection coefficient magnitude versus frequency for the Chebyshev multisection matching transformers of Example 5.7.*

- Note that the **bandwidth** defined by  $f_m$  **increases** as the **number of sections  $N$**  is increased.
- Note also that the reflection coefficient is **not necessarily zero** at the design frequency  $f_0$  !!!

Instead, we find:

$$|\Gamma(f=f_0)| = \begin{cases} 0 & \text{for odd-valued } N \\ \Gamma_m & \text{for even-valued } N \end{cases}$$