

$$1. \quad P(t) = \frac{10^5 P(0)}{P(0) + (10^5 - P(0)) e^{-0.01 t}}$$

Know $P(0) = 0$, so

$$P(t) = \frac{10^5 \cdot 0}{\dots} = \underline{\underline{0}}$$

$$2. \quad \lim_{n \rightarrow \infty} \frac{n}{n+1} = \lim_{n \rightarrow \infty} \frac{1}{1 + \frac{1}{n}} = \frac{1}{1+0} = \underline{\underline{1}}$$

3. $\sin \frac{n\pi}{2} = 0$ IF n EVEN, ALTERNATES \pm IF n ODD
 \rightarrow LIM DOES NOT EXIST

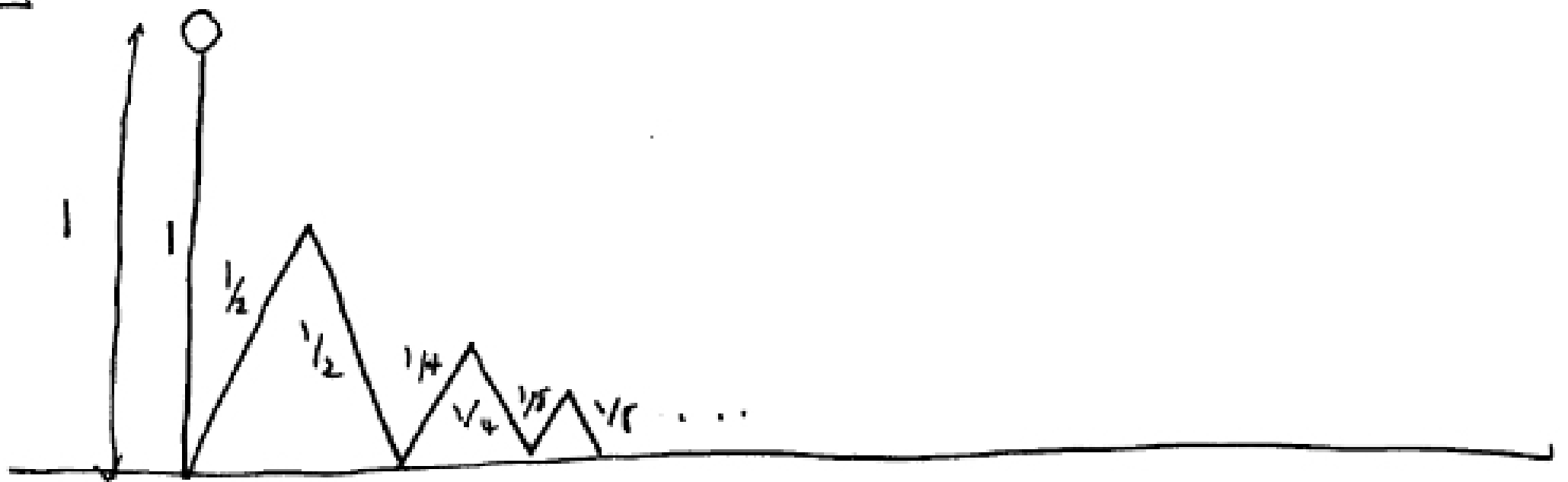
$$4. \quad \begin{aligned} \sqrt{2} &= 2 \cdot \frac{1}{10} + 2 \cdot \frac{1}{10^2} + 2 \cdot \frac{1}{10^3} + 2 \cdot \frac{1}{10^4} + \dots \\ &= \frac{2}{10} \left(1 + \frac{1}{10} + \frac{1}{10^2} + \frac{1}{10^3} + \dots \right) \\ &= \frac{1}{5} \left(\frac{1}{1 - \frac{1}{10}} \right) = \frac{1}{5} \cdot \frac{10}{9} = \underline{\underline{\frac{2}{9}}} \end{aligned}$$

5. $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \dots$ IS THE HARMONIC SERIES,
 WHICH WE SHOWED DOESN'T CONVERGE

$$6. \quad \begin{aligned} \sum_{n=0}^{\infty} \left(\frac{1}{2^n} - \frac{1}{3^n} \right) &= \sum_{n=0}^{\infty} \frac{1}{2^n} - \sum_{n=0}^{\infty} \frac{1}{3^n} \\ &= \sum_{n=0}^{\infty} \left(\frac{1}{2} \right)^n - \sum_{n=0}^{\infty} \left(\frac{1}{3} \right)^n \\ &= \frac{1}{1 - \frac{1}{2}} - \frac{1}{1 - \frac{1}{3}} = \frac{2}{2-1} - \frac{3}{3-1} \\ &= 2 - \frac{3}{2} = \underline{\underline{\frac{1}{2}}} \end{aligned}$$

#15;

(2)



TOTAL DISTANCE TRAVELLED =

$$1 + 2 \cdot \frac{1}{2} + 2 \cdot \frac{1}{4} + 2 \cdot \frac{1}{8} + \dots$$
$$= 1 + (1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} \dots) = 1 + \frac{1}{1 - \frac{1}{2}} = 1 + 2 = \underline{3} \text{ m.}$$

7) Straightforward use of error bounds from the Integral Test:

$$|S - S_{10}| = |R_{10}| \leq \int_{10}^{\infty} \frac{1}{x^3} dx = \lim_{t \rightarrow \infty} \left[-\frac{1}{2x^2} \right]_{10}^t$$

↑
TRUE SUM

$$= \boxed{.005}$$

8) $\lim_{n \rightarrow \infty} \frac{\sin(\frac{1}{\sqrt{n}})}{\frac{1}{\sqrt{n}}} = 1$, so by the Limit Comparison

Test, $\sum \sin(\frac{1}{\sqrt{n}})$ has same behavior as $\sum \frac{1}{\sqrt{n}}$.

But $\sum \frac{1}{\sqrt{n}}$ is a divergent p-series ($p = \frac{1}{2} < 1$),

so $\sum_{n=1}^{\infty} \sin(\frac{1}{\sqrt{n}})$ diverges by L.C.T. w/ $\sum \frac{1}{\sqrt{n}}$

9) I) If $\sum a_n$ converges, then $a_n \rightarrow 0$. TRUE

II) If $\sum b_n$ converges, $b_n > 0$, then

$\sum \frac{b_n}{n^2}$ converges. TRUE ($\frac{b_n}{n^2} \leq b_n$, Comp. Test)

III) If $\sum a_n$ converges and $a_n = f(n)$,

then $\lim_{x \rightarrow \infty} f(x) = 0$. FALSE (This is tricky.)

Consider the function $\sin(x\pi) = f(x)$. Then

$f(n) = \sin(n\pi) = 0$, so $f(n) \rightarrow 0$ as $n \rightarrow \infty$, but

$f(x)$ oscillates between ± 1 as $x \rightarrow \infty$.