

## Lecture 9

Single particle:  $\vec{F} = m \vec{a}$

New idea compare time before to time after  $\Delta T$

Impulse causes momentum change

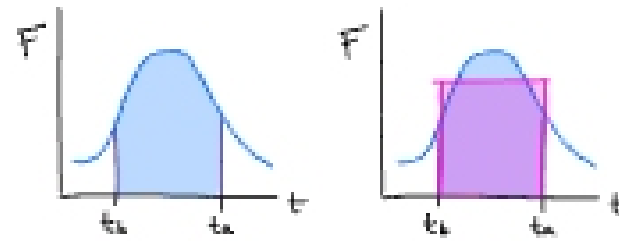
System of particles: Combine Newton's Second and Third Laws  $\vec{F} = \frac{d\vec{p}}{dt}$

Momentum of a single part  $\vec{p} = m \vec{v}$  kg m s<sup>-1</sup>

Force:  $\vec{F} = m \vec{a} = m \frac{d\vec{v}}{dt} = \frac{d\vec{p}}{dt}$

Newton's Second Law:  $\int \vec{F} dt = \int d\vec{p}$

Impulse = momentum (time after) - momentum (time before)



Momentum and Impulse

Obeys a conservation law

Simplifies complicated motions

Describes Collisions

Basis of rocket propulsion and space travel

System of particles: Newton's Second Law

The momentum of a system of  $N$  particles is defined as the sum of individual momenta of the particles

$$\vec{P}_{sys} \equiv \sum_{i=1}^{N} \vec{P}_i = \sum_{i=1}^{N} m_i \vec{v}_i$$

Force changes the momentum of the system

$$\vec{F} = \frac{d\vec{P}_{sys}}{dt} = \sum_{i=1}^{N} \frac{d\vec{P}_i}{dt} = \frac{d\vec{P}_{sys}}{dt}$$

Internal forces in a system of particles is zero

The internal force on the  $i$ th particle is sum of the internal interaction forces with all the other particles

$$\vec{F}_{int,i} = \sum_{j \neq i} \vec{F}_{j,i}$$

The sum of the internal forces on each particle in the system is

$$\vec{F}_{int} = \sum_{i=1}^N \vec{F}_{int,i} = \sum_{i=1}^N \sum_{j \neq i} \vec{F}_{j,i}$$

Newton's Third Law: internal forces cancel in pairs

$$\vec{F}_{i,j} = -\vec{F}_{j,i}$$

So the sum of the internal forces on the system is zero

$$\vec{F}_{int} = \vec{0}$$

Newton's second and third laws for system of particles

Newton's third law: the force on a system of particles is the external force because internal forces cancel in pairs  $\vec{F} = \vec{F}_{ext} + \vec{F}_{int} = \vec{F}_{ext}$

Newton's second law: The total external force is equal to the rate of change of the momentum of the system  $\vec{F}_{ext} = \frac{d\vec{P}_{sys}}{dt}$

Position of center of mass system of particles

Mass for collection of discrete bodies (system):  $M_{sys} = \sum_{i=1}^N M_i$

Position of center of mass  $\vec{R}_{cm} = \frac{1}{M_{sys}} \sum_{i=1}^N M_i \vec{r}_i$