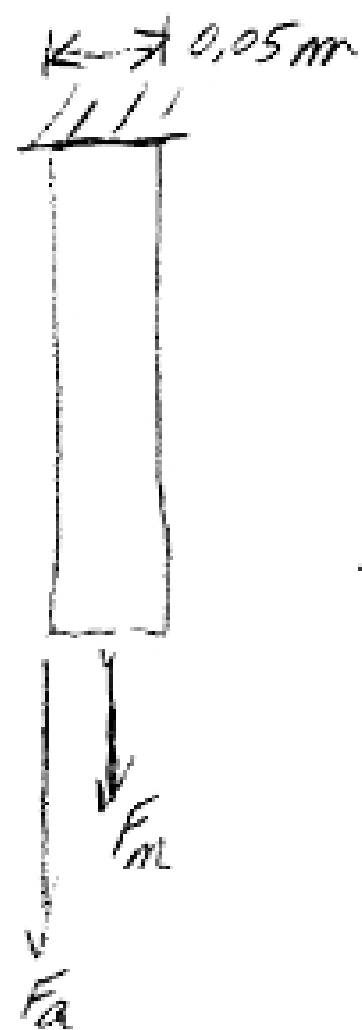


# FATIGUE



$$\sigma_{yp} = 280 \text{ MPa} \quad \sigma_u = 350 \text{ MPa}$$

$$P_{\text{mean}} = 100 \text{ kN}$$

FATIGUE STRENGTH =  $210 \text{ MPa} @ 10^6 \text{ cyc.}$

DETERMINE THE AMPLITUDE OF THE CYCLING FORCE FOR NO FATIGUE FAILURE AT  $10^6$  CYCLES

$$M_a = e F_a = 0.025 F_a$$

$$\sigma_a = \frac{M_a c}{I} = \frac{(0.025) F_a (0.025)}{(0.05)^4 / 12} = 1200 F_a$$

$$\sigma_m = \frac{F_m}{A} = \frac{100,000}{(0.05)^2} = 40 \text{ MPa}$$

APPLY SODERBERG CRITERIA

$$\frac{\sigma_a}{\sigma_{cr}} + \frac{\sigma_m}{\sigma_{yp}} = 1$$

$$\frac{1200 F_a}{210 \times 10^6} + \frac{40 \times 10^6}{280 \times 10^6} = 1$$

$$F_a = \left(1 - \frac{40}{280}\right) \left(\frac{210 \times 10^6}{1200}\right) = 150,000 \text{ N} \\ = 150 \text{ kN}$$

APPLY MODIFIED GOODMAN CRITERIA

$$\frac{\sigma_a}{\sigma_{cr}} + \frac{\sigma_m}{\sigma_u} = 1$$

$$\frac{1200 F_a}{210 \times 10^6} + \frac{40 \times 10^6}{350 \times 10^6} = 1$$

$$F_a = \left(1 - \frac{40}{350}\right) \left(\frac{210 \times 10^6}{1200}\right) = 155000 \text{ N}$$

$$= 155 \text{ kN}$$

APPLY GERBER CRITERIA

$$\frac{\sigma_a}{\sigma_{cr}} + \left(\frac{\sigma_m}{\sigma_u}\right)^2 = 1$$

$$\frac{1200 F_a}{210 \times 10^6} + \left(\frac{40 \times 10^6}{350 \times 10^6}\right)^2 = 1$$

$$F_a = \left(1 - \left(\frac{40}{350}\right)^2\right) \left(\frac{210 \times 10^6}{1200}\right) = 172714 \text{ N}$$

$$= 173 \text{ kN}$$

APPLY SAE CRITERIA

$$\frac{\sigma_a}{\sigma_{cr}} + \frac{\sigma_m}{\sigma_f} = 1$$

$$\frac{1200 F_a}{210 \times 10^6} + \frac{40 \times 10^6}{350 \times 10^6} = 1$$

(SAME AS MODIFIED GOODMAN)

MODIFIED GOODMAN  
SAE

155 kN

SODERBERG

150 kN

GERBER

173 kN

## COMBINED LOADING

USE MODIFIED STATIC FAILURE CRITERIA

## MAXIMUM DISTORTIONAL ENERGY THEORY

$$(\sigma_{xa} - \sigma_{ya})^2 + (\sigma_{ya} - \sigma_{za})^2 + (\sigma_{za} - \sigma_{xa})^2 + 6(\tau_{xya}^2 + \tau_{yza}^2 + \tau_{zxa}^2) = 2\sigma_{ea}^2$$

$$(\sigma_{xm} - \sigma_{ym})^2 + (\sigma_{ym} - \sigma_{zm})^2 + (\sigma_{zm} - \sigma_{xm})^2 + 6(\tau_{xym}^2 + \tau_{yzm}^2 + \tau_{zxm}^2) = 2\sigma_{em}^2$$

$$(\sigma_{1a} - \sigma_{2a})^2 + (\sigma_{2a} - \sigma_{3a})^2 + (\sigma_{3a} - \sigma_{1a})^2 = 2\sigma_{ea}^2$$

$$(\sigma_{1m} - \sigma_{2m})^2 + (\sigma_{2m} - \sigma_{3m})^2 + (\sigma_{3m} - \sigma_{1m})^2 = 2\sigma_{em}^2$$

## MAX PRINCIPAL STRESS THEORY

$$\frac{\sigma_{1a}}{\sigma_{1a}} + \frac{\sigma_{1m}}{\sigma_{1a}} = \pm 1 \quad \text{OR} \quad \frac{\sigma_{1a}}{\sigma_{yp}} + \frac{\sigma_{1m}}{\sigma_{yp}} = \pm 1$$

$$\frac{\sigma_{2a}}{\sigma_{2a}} + \frac{\sigma_{2m}}{\sigma_{2a}} = \pm 1 \quad \text{OR} \quad \frac{\sigma_{2a}}{\sigma_{yp}} + \frac{\sigma_{2m}}{\sigma_{yp}} = \pm 1$$

## MAXIMUM SHEARING STRESS

(σ<sub>1</sub> & σ<sub>2</sub> OPPOSITE SIGN)

$$\frac{\sigma_{1a} + \sigma_{1m}}{\sigma_{yp}} - \frac{\sigma_{2a} + \sigma_{2m}}{\sigma_{yp}} = \pm 1$$

SAME SIGN

$$|(\sigma_{1a} + \sigma_{1m}) - (\sigma_{2a} + \sigma_{2m})| = \sigma_{yp}$$