

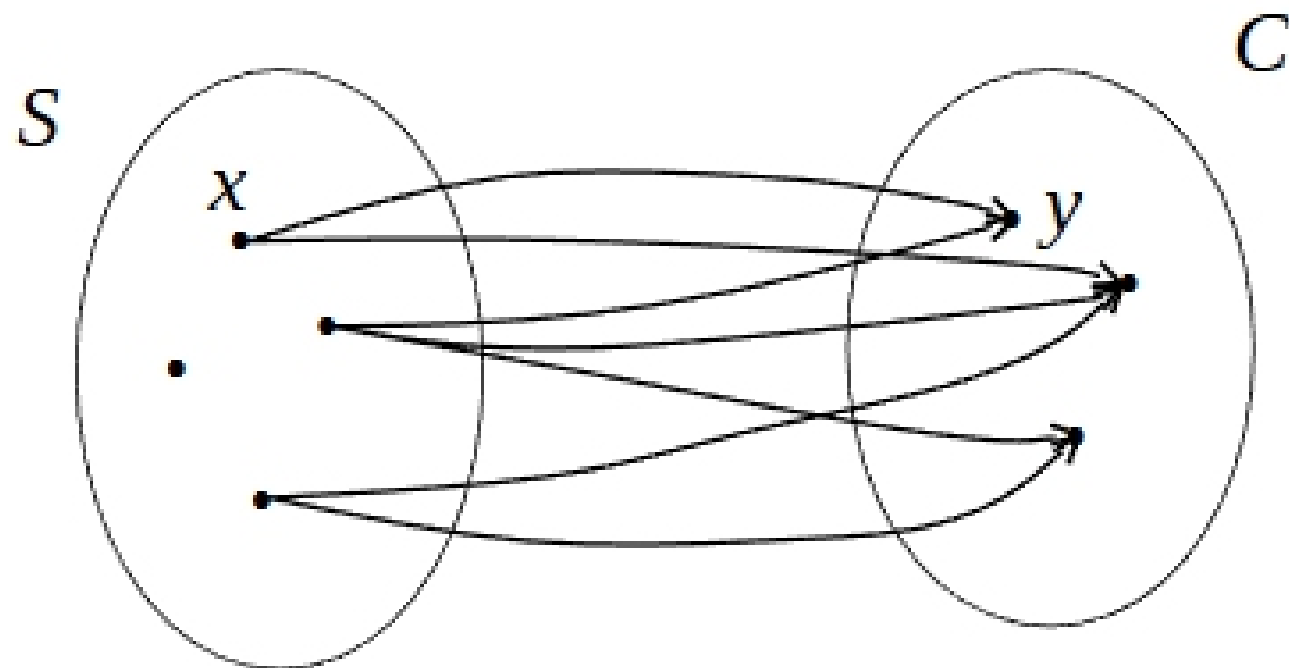
Today's topics:

- The notion of a relation
- properties of relations on a set

Relations

- A “**relation**” is a fundamental mathematical notion expressing a relationship between sets
- It's an **abstract** notion useful for modeling many different relationships

Example. Let S be set of UCF students, and C be a set of classes. Then we can consider the relation “is taking class” from S to C



This relation can be described by the set of pairs:

“is taking class” = $\{(x, y) \mid x \in S, y \in C \text{ and student } x \text{ is taking class } y\}$

More examples of relations:

- “parent-of”
- “child-of”
- “likes”
- “meet one another today”
- “less than” = $\{(a, b) \mid a, b \in A \text{ and } a < b\}$
where $A = \{1, 2, \dots, 10\}$
- “equal” = $\{(a, b) \mid a, b \in \text{Power}(A) \text{ and } |a| = |b|\}$
- “subset” = $\{(a, b) \mid a, b \in \text{Power}(A) \text{ and } a \subseteq b\}$
- If \mathbb{R} is set of real numbers, $\mathbb{R} \times \mathbb{R}$ is set of points (x, y) in plane.
“circle” = $\{(x, y) \mid x, y \in \mathbb{R} \text{ and } x^2 + y^2 = 1\}$