



CSE332: Data Abstractions

Lecture 27: A Few Words on NP

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Easily one of the most important questions in Computer Science:

Does $P=NP$?

- ▶ Of course, we need to go into what these terms mean
- ▶ P and NP are *classes* of problems
 - ▶ P : Class of problems that can be solved in polynomial time
 - ▶ NP : Class of problems where an answer can be *verified* in polynomial time
 - ▶ We'll get into what that means
- ▶ The question is, are these sets equivalent?
 - ▶ A question that computer scientists & mathematicians have been grappling with for a long time
 - ▶ Most believe that $P \neq NP$, but no one's proven it
 - ▶ One such proof recently in the news ($P \neq NP$; probably not valid)

Wow, that's fantastic... who cares?

- ▶ P=NP would mean that many 'difficult' problems that could previously only be solved in exponential time could now be solved in polynomial time
 - ▶ Some algorithms (such as cryptography) are based around the 'difficulty' of brute-forcing it, but the ease of which an answer can be verified
 - ▶ You can break many online encryptions now... with enough computing power
 - ▶ Say, an enormous # of computers
 - ▶ Or one computer running for several centuries
 - ▶ And you don't break the scheme itself; you break it for a single session
 - ▶ If P=NP, much of existing cryptography would (in theory) be insecure