

## Beyond Physical Memory: Policies

In a virtual memory manager, life is easy when you have a lot of free memory. A page fault occurs, you find a free page on the free-page list, and assign it to the faulting page. Hey, Operating System, congratulations! You did it again.

Unfortunately, things get a little more interesting when little memory is free. In such a case, this **memory pressure** forces the OS to start **paging out** pages to make room for actively-used pages. Deciding which page (or pages) to **evict** is encapsulated within the **replacement policy** of the OS; historically, it was one of the most important decisions the early virtual memory systems made, as older systems had little physical memory. Minimally, it is an interesting set of policies worth knowing a little more about. And thus our problem:

### THE CRUX: HOW TO DECIDE WHICH PAGE TO EVICT

How can the OS decide which page (or pages) to evict from memory? This decision is made by the replacement policy of the system, which usually follows some general principles (discussed below) but also includes certain tweaks to avoid corner-case behaviors.

## 22.1 Cache Management

Before diving into policies, we first describe the problem we are trying to solve in more detail. Given that main memory holds some subset of all the pages in the system, it can rightly be viewed as a **cache** for virtual memory pages in the system. Thus, our goal in picking a replacement policy for this cache is to minimize the number of **cache misses**; that is, to minimize the number of times that we have to go to disk to fetch the desired page. Alternately, one can view our goal as maximizing the number of **cache hits**, i.e., the number of times a page that is read or written is found in memory.

Knowing the number of cache hits and misses let us calculate the **average memory access time (AMAT)** for a program (a metric computer architects compute for hardware caches [HP06]). Specifically, given these values, we can compute the AMAT of a program as follows:

$$AMAT = (Hit\% \cdot T_M) + (Miss\% \cdot T_D) \quad (22.1)$$

where  $T_M$  represents the cost of accessing memory, and represents  $T_D$  the cost of accessing disk.

For example, let us imagine a machine with a (tiny) address space: 4KB, with 256-byte pages. Thus, a virtual address has two components: a 4-bit VPN (the most-significant bits) and an 8-bit offset (the least-significant bits). Thus, a process in this example can access  $2^4$  or 16 total virtual pages. In this example, the process generates the following memory references (i.e., virtual addresses): 0x000, 0x100, 0x200, 0x300, 0x400, 0x500, 0x600, 0x700, 0x800, 0x900. These virtual addresses refer to the first byte of each of the first ten pages of the address space (the page number being the first hex digit of each virtual address).

Let us further assume that every page except virtual page 3 are already in memory. Thus, our sequence of memory references will encounter the following behavior: hit, hit, hit, miss, hit, hit, hit, hit, hit, hit. We can compute the **hit rate** (the percent of references found in memory): 90%, as 9 out of 10 references are in memory. The **miss rate** is obviously 10%.

To calculate AMAT, we simply need to know the cost of accessing memory and the cost of accessing disk. Assuming the cost of accessing memory ( $T_M$ ) is around 100 nanoseconds, and the cost of accessing disk ( $T_D$ ) is about 10 milliseconds, we have the following AMAT:  $0.9 \cdot 100ns + 0.1 \cdot 10ms$ , which is  $90ns + 1ms$ , or 1.00009 ms, or about 1 millisecond. If our hit rate had instead been 99.9%, the result is quite different: AMAT is 10.1 microseconds, or roughly 100 times faster. As the hit rate approaches 100%, AMAT approaches 100 nanoseconds.

Unfortunately, as you can see in this example, the cost of disk access is so high in modern systems that even a tiny miss rate will quickly dominate the overall AMAT of running programs. Clearly, we need to avoid as many misses as possible or run slowly, at the rate of the disk. One way to help with this is to carefully develop a smart policy, as we now do.

## 22.2 The Optimal Replacement Policy

To better understand how a particular replacement policy works, it would be nice to compare it to the best possible replacement policy. As it turns out, such an **optimal** policy was developed by Belady many years ago [B66] (he originally called it MIN). The optimal replacement policy leads to the fewest number of misses overall. Belady showed that a simple (but, unfortunately, difficult to implement!) approach that replaces the page that will be accessed *furthest in the future* is the optimal policy, resulting in the fewest-possible cache misses.

**TIP: COMPARING AGAINST OPTIMAL IS USEFUL**

Although optimal is not very practical as a real policy, it is incredibly useful as a comparison point in simulation or other studies. Saying that your fancy new algorithm has a 80% hit rate isn't meaningful in isolation; saying that optimal achieves an 82% hit rate (and thus your new approach is quite close to optimal) makes the result more meaningful and gives it context. Thus, in any study you perform, knowing what the optimal is lets you perform a better comparison, showing how much improvement is still possible, and also when you can *stop* making your policy better, because it is close enough to the ideal [AD03].

Hopefully, the intuition behind the optimal policy makes sense. Think about it like this: if you have to throw out some page, why not throw out the one that is needed the furthest from now? By doing so, you are essentially saying that all the other pages in the cache are more important than the one furthest out. The reason this is true is simple: you will refer to the other pages before you refer to the one furthest out.

Let's trace through a simple example to understand the decisions the optimal policy makes. Assume a program accesses the following stream of virtual pages: 0, 1, 2, 0, 1, 3, 0, 3, 1, 2, 1. Table 22.1 shows the behavior of optimal, assuming a cache that fits three pages.

In the table, you can see the following actions. Not surprisingly, the first three accesses are misses, as the cache begins in an empty state; such a miss is sometimes referred to as a **cold-start miss** (or **compulsory miss**). Then we refer again to pages 0 and 1, which both hit in the cache. Finally, we reach another miss (to page 3), but this time the cache is full; a replacement must take place! Which begs the question: which page should we replace? With the optimal policy, we examine the future for each page currently in the cache (0, 1, and 2), and see that 0 is accessed almost immediately, 1 is accessed a little later, and 2 is accessed furthest in the future. Thus the optimal policy has an easy choice: evict page 2, resulting in pages 0, 1, and 3 in the cache. The next three references are hits, but then

Access	Hit/Miss?	Evict	Resulting Cache State
0	Miss		0
1	Miss		0, 1
2	Miss		0, 1, 2
0	Hit		0, 1, 2
1	Hit		0, 1, 2
3	Miss	2	0, 1, 3
0	Hit		0, 1, 3
3	Hit		0, 1, 3
1	Hit		0, 1, 3
2	Miss	3	0, 1, 2
1	Hit		0, 1, 2

Table 22.1: Tracing the Optimal Policy