

CSE 341: Programming Languages

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Spring 2008

Lecture 12— Parametric Polymorphism; Equivalence

Today

Two more “conceptual” topics

- Higher density of more abstract concepts as course progresses
- Think about the theory and how languages “fit together”, not just how do I “code something up”

1. Parametric polymorphism

- Also: Type constructors (e.g., ML's `list` and `option`)

2. Equivalence

- When are two functions or other expressions “the same”

Parametric Polymorphism

Fancy phrase for “forall types” or sometimes “generics.” In ML since mid-80s and now in Java, C#, VB, etc.

- (C++ templates are more like macros (later)).

In ML, there's an implicit “for all” at the beginning of any type with 'a, 'b, etc. Example:

$$('a * 'b) \rightarrow ('b * 'a)$$

really means:

$$\text{forall } 'a, 'b . (('a * 'b) \rightarrow ('b * 'a))$$

(though forall is just for lecture purposes; it is not in ML)

We can *instantiate* the *type variables* to get a *less general* type. For example, with `string` for 'a and `int->int` for 'b we get:

$$(\text{string} * (\text{int} \rightarrow \text{int})) \rightarrow ((\text{int} \rightarrow \text{int}) * \text{string})$$