

VI-1:

Number (#)	L (cm)
1	176.0
2	177.5
3	161.0
4	159.0
5	160.9
6	162.4
7	175.0
8	174.0
9	174.0
10	175.0

Calculation of mean & standard deviation can be done using excel

For the first 3 measurements:

-Average value of L: 171.5cm

-Standard deviation of L: 9.124144cm

-Standard deviation of the mean of L: 5.267826995cm

Calculation of standard deviation of the mean:

$$\sigma_x = \frac{\sigma_x}{\sqrt{N}} = \frac{9.124144}{\sqrt{3}} = 5.267826995 \text{ cm}$$

For the first 5 measurements:

-Average value of L: 166.88cm

-Standard deviation of L: 9.060739484cm

-Standard deviation of the mean of L: 4.052085666cm

For all 10 measurements:

- Average value of L: 169.48cm
- Standard deviation of L: 7.558042075cm
- Standard deviation of the mean of L: 2.390062737cm

$$L \pm \sigma_L = 169 \pm 2$$

As more measurements were taken, standard deviation got smaller, which means there is less variability from the mean as more measurements are taken.

VI-2:

Minimum graduation on ammeter	1.0 mA
Minimum graduation on voltmeter	0.5 V
Parallax reading of current	29 mA
Parallax reading of voltage	5 V
Measured Current	30 mA
Measured voltage	4.5 V
R using DVM	147.8 ohms

Calculation of uncertainty of current (σ_I):

$$\sigma_I = \sqrt{(\sigma_I \text{ due to parallax})^2 + (\sigma_I \text{ due to meter graduations})^2}$$

$$\sigma_I \text{ due to parallax} = \text{Actual value} - \text{parallax value} = 30 - 29 = 1 \text{ mA}$$

$$\sigma_I \text{ due to parallax} = 0.5 \times \text{smallest graduation} = 0.5 \times 1 = 0.5 \text{ mA}$$

Therefore,

$$\sigma_I = \sqrt{(1)^2 + (0.5)^2} = 1.118033989 \text{ mA}$$

Same calculation is applied to the uncertainty of voltage

$$\sigma_V = 0.5590169944 \text{ V}$$

Using equation $R = V/I$:

$$V = 4.5 \text{ volts}, I = 30 \text{ mA}$$

$$R = (4.5 \text{ volts}) / (30 \text{ mA}) = 0.150 \text{ volts/ mA} = 150 \Omega$$

With the equation $C = \frac{A}{B}$,

$$\frac{\sigma_C}{C} = \sqrt{\left(\frac{\sigma_A}{A}\right)^2 + \left(\frac{\sigma_B}{B}\right)^2}$$

Thus, with the equation $R = \frac{V}{I}$,

$$\frac{\sigma_R}{R} = \sqrt{\left(\frac{\sigma_V}{V}\right)^2 + \left(\frac{\sigma_I}{I}\right)^2}$$

$$\sigma_R = R \sqrt{\left(\frac{\sigma_V}{V}\right)^2 + \left(\frac{\sigma_I}{I}\right)^2} = (150) \sqrt{\left(\frac{1.118033989}{4.5}\right)^2 + \left(\frac{0.5590169944}{30}\right)^2} = 37.3724683 \Omega$$

$$R \pm \sigma_R = 150 \pm 40 \Omega$$

The calculated value of R does agree with the measured value of the resistance 147.8Ω .