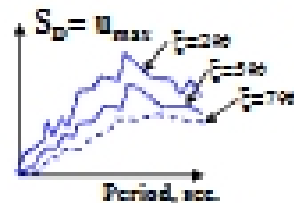


# Elastic Design Response Spectra

Envelope of a computed peak dynamic response parameter for single degree of freedom elastic systems having a range of periods, for a given ground motion and viscous damping ratio

$$m\ddot{a}(t) + 2\xi\omega_n\dot{w}(t) + Kd(t) = -m\ddot{a}_g(t)$$



### Uses

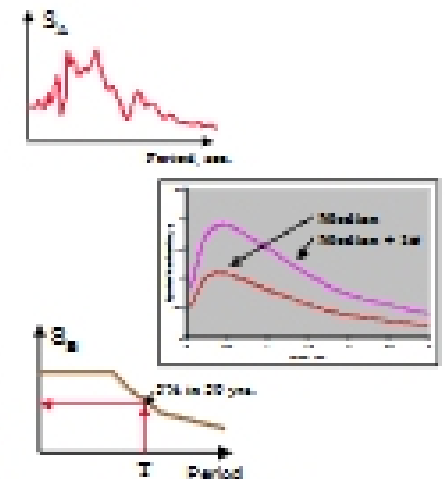
- Characterize ground motions and assess demands on various types of simple structures.
- Basis for computing design displacements and forces in SDOF and MDOF systems expected to remain elastic.
- Basis for developing design forces and displacements in nonlinear systems (two approaches):
  - Modified elastic spectrum to account for nonlinearity
  - Equivalent elastic SDOF system



# Design Response Spectrum

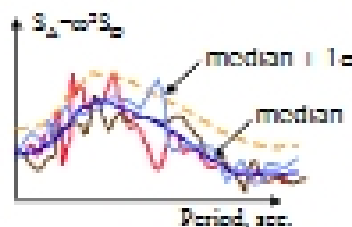
### Topics

- Developing design spectra from site specific ground motion time histories
- Selection of damping values
- Plotting formats
- Analytic relations for developing Elastic Design Response Spectrum
  - Deterministic
    - Statistical "attenuation" relationships
    - Empirical empirical relationships (e.g., Newmark-Hall methods)
  - Uniform Hazard Spectrum
    - Block approach (from UHLS) favored (more used in current codes)
    - Current spectra formulations based on codes (how do they relate to theory?)



## Smooth Design Response Spectrum from Ground Motion Records

- Response Spectrum for actual ground motions are quite irregular.
  - Don't use individual spectrum for design
  - They can be used for analysis to assess response to a particular earthquake.

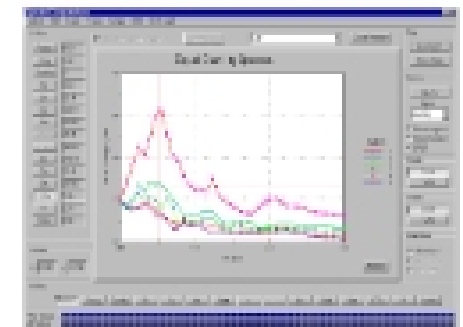
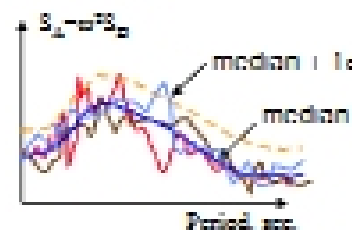


- Use suites of ground motions representing:
  - A specific deterministic design earthquake (e.g., M = 7 at 10 km)
  - Multiple simulated design response spectrum (e.g., multi code spectrum)
  - A range of earthquake types corresponding to the design period seismic hazard of the site.
- The design response spectrum is obtained statistically from all records. The resulting "median" spectrum will be relatively smooth. The COV or Standard Deviation ( $\sigma_s$ ) can be used to establish a design spectrum with a desired probability of exceedence.
- Note: Various programs do this automatically.



## Generate Smooth Spectrum from Records

- PEER NGA Database will search for particular types of records and plot scaled response spectrum. Can download tables of spectral values for different periods and damping ratios
- Bispec and other programs
  - Permit user to input a suite of ground motion records and will find median and median plus 'x' sigma values



## Viscous Damping

Viscous damping is a convenient analytical concept to account for general energy dissipation in a system and analytical uncertainties.

- Friction between and with structural and non-structural elements.
- Localized yielding due to stress concentrations and residual stresses under low loading and gross yielding under higher loads.
- Energy radiation through foundation.
- Aeroelastic damping.
- Viscous damping.
- Analytical modeling errors.

Damping is generally a function of:

- Material
- Amplitude (stress)
- Type of nonstructural elements
- Type of foundation and supporting soils
- Frequency
- Type of connection
- Complexity of model (different parts of structure will be responding differently)

Constant viscous damping is a simplification.

Damping can produce substantial forces that are only crudely modeled compared to inertial and restoring forces.

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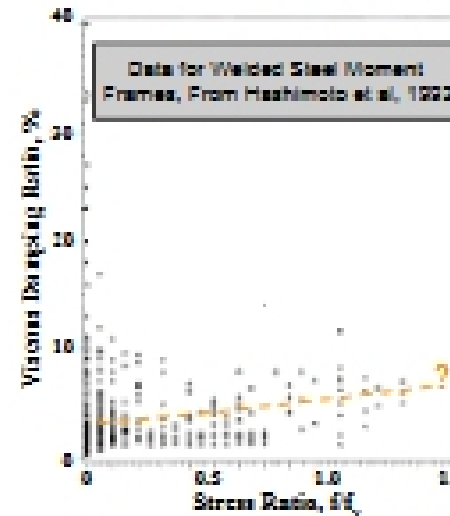
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## Data on Viscous Damping



### References

- NRC, "Regulatory Guide 1.61, Damping Values for Seismic Design of Nuclear Power Plants," U.S. Atomic Energy Commission, Oct. 1973.
- Goetz, D., "Damping in Building Structures During Earthquakes, Test Data and Modeling," NUREG/CR 3006, Jan. 1980.
- Hashimoto, F. et al, "Review of Regulatory Guide 1.61 Structure Damping Values for Elastic Seismic Analysis of Nuclear Power Plants," Nuclear Regulatory Commission, 1992

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## Recommended Design Damping Values

- Many codes stipulate 5% viscous damping, unless a more properly substantiated value can be used.
- Note that actual damping values for many systems, even at higher levels of excitation are less than 5%.

Structure Type	Working Stress Range (maximum stress about 1.0 yield stress)			Non-Linear Range (Full Yield)		
	NBC 1991	ASCE	Eurocode	NBC 1991	ASCE	Eurocode
Welded Steel Moment	2	2 to 8	2.5	5	5 to 7	5**
Welded Steel Moment	4	5 to 7	4.5	7	7 to 15	8
Welded Steel Moment	2	2 to 8	100	5	5 to 7	100
Welded Steel Moment	4	2 to 8*	8	7	7 to 10	7

\* Lightly cracked sections represent lower values in range

\*\* Values listed are minimum values for welded steel

\*\*\* values to be determined when sufficient data is available

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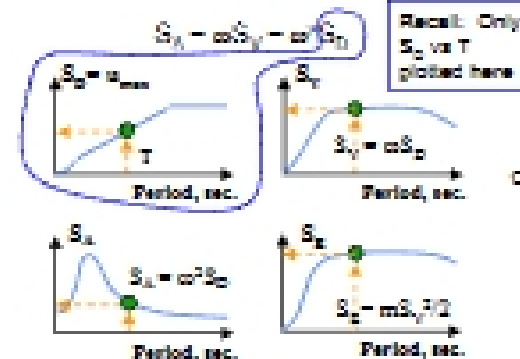
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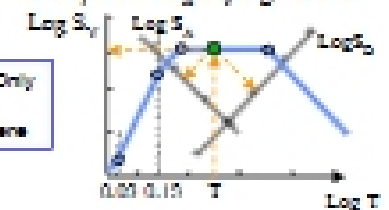
## Formats for Plotting Spectra

A variety of formats used

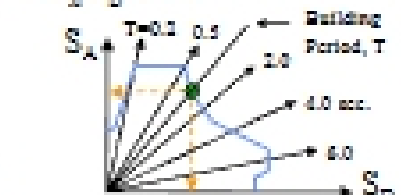
- $\hat{S}_A$ ,  $\hat{S}_V$ ,  $\hat{S}_D$  and  $\hat{S}_T$



- Tripartite  $S_A$ - $S_V$ - $S_D$  Format



- $S_A$ - $S_D$  Format



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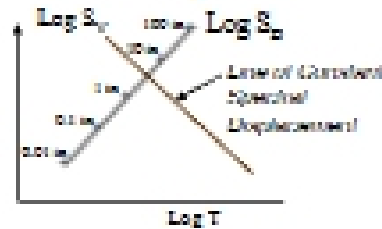
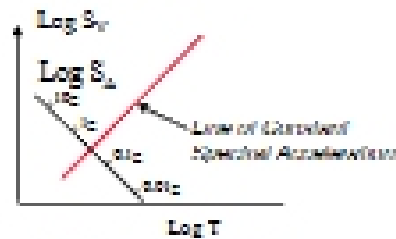
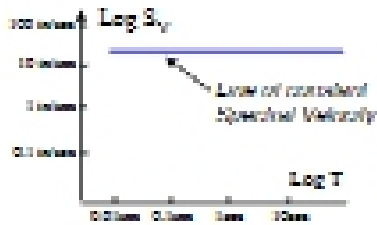
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## Basis of Tripartite Graph Paper

$$S_v = S_a / \omega = S_a T / 2\pi$$

$$= \omega S_d = 2\pi S_d T^{-1}$$

- line of constant spectral acceleration  
line a slope of 1 on a log-log plot of  $S_v$  vs.  $T$
- line of constant spectral displacement  
line a slope of -1 on log-log plot of  $S_v$  vs.  $T$



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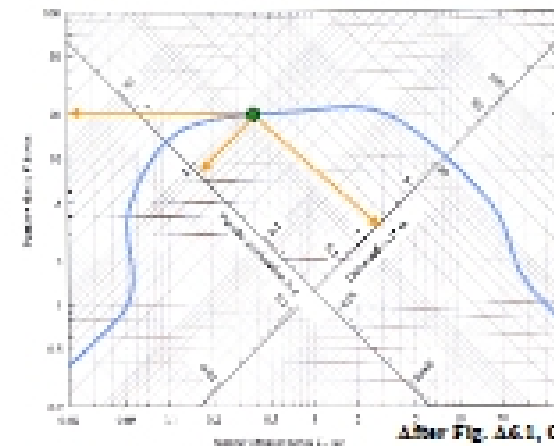
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## Tripartite Response Spectrum



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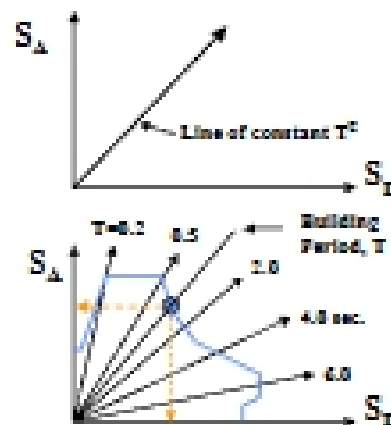
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## $S_A$ - $S_D$ Format

- An alternative form of plotting spectra has been introduced recently and has started to appear in building codes.
- Intent is to plot information on acceleration (force) and displacement on same graph with out complexity of tripartite paper
- Based on:  $S_a = \omega^2 S_d \rightarrow \omega^2 = S_a / S_d$
- Used to interpret nonlinear response in conjunction with "Capacity Spectrum" and "Yield Point Spectrum" Methods Discussed later



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## Analytic Relations for Developing Elastic Design Response Spectrum

- **Deterministic Approaches**
  - Statistical attenuation relations for a given magnitude, distance, soil condition, fault type, etc.
  - Simplified empirical methods by Newmark and others for a given peak ground acceleration
- **Spectra based on Probabilistic Hazard Analysis**
  - Uniform hazard methods (focus on USGS data)
  - NEHRP Tentative Provisions for Seismic Regulations for New Buildings

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