

Math 128

Midterm Examination 2 – October 21, 2008

Name \_\_\_\_\_

6 problems, 100 points.

**Instructions:** Show all work – partial credit will be given, and “Answers without work are worth credit without points.” You don’t have to simplify your answers. You may use a simple calculator that is not graphing or programmable. You may have a 3x5 card, but no other notes.

1. (9 points each) Evaluate the following:

(a)  $\int x \cos 3x \, dx$

(b)  $\int_1^e \frac{\ln x}{x} \, dx$

(c)  $\int_1^{\infty} \frac{x}{(x^2 + 3)^5} dx$

2. Consider the function  $f(x) = \cos x^2$ .

(a) (4 points) Calculate  $M_3$  for the integral  $\int_{-2}^1 \cos x^2 dx$ .

(b) (8 points) Find an upper bound  $A$  for  $|f''(x)| = \left| \frac{d^2}{dx^2} \cos x^2 \right|$  on the interval  $[-2, 1]$ .

(c) (4 points) Using your result from part (b), find an  $n$  so that the midpoint rule approximation  $M_n$  is accurate to 0.0025 for the integral  $\int_{-2}^1 \cos x^2 dx$ .