

# Electromagnetic waves

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**Note: These slides are not a complete representation of the lecture. Details are presented on whiteboard.**

- Maxwell's equations, review
- Wave equation
- Electromagnetic waves
- Speed of em waves (light)
- Antenna, radio waves
- Electromagnetic spectrum

## Demonstrations

- Radio emission from dipole transmitter,
  - Receiver with small light bulb
  - Length of antenna
  - Orientation and distance of receiving antenna
  - Magnetic loop antenna (with LC circuit)
- Microwave transmitter
  - Polarized waves get absorbed or reflected by grid when grid is oriented in direction of dipole.

## Maxwell's Equations

$$\oint_S \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

- Gauss's law (electric)

$$\oint_S \vec{B} \cdot d\vec{A} = 0$$

- Gauss's law in Magnetism

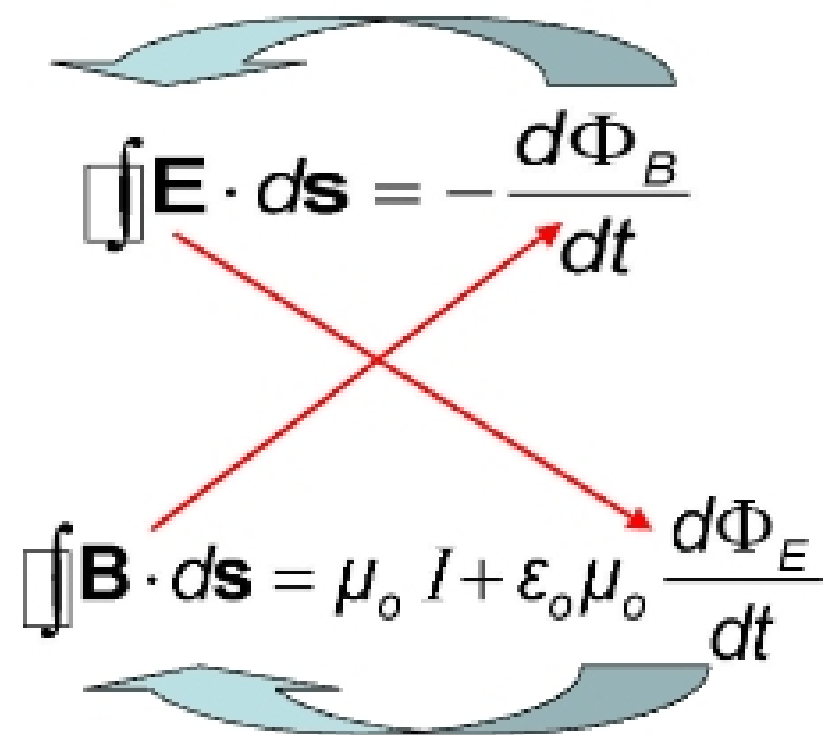
$$\oint \vec{E} \cdot d\vec{s} = -\frac{d\Phi_B}{dt}$$

- Faraday's Law

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I + \epsilon_0 \mu_0 \frac{d\Phi_E}{dt}$$

- Ampere-Maxwell Law

Connections between Maxwell's equations:



## Derivation of Speed – Some Details

- From Maxwell's equations applied to empty space, the following partial derivatives can be found:

$$\frac{\partial^2 E}{\partial x^2} = \mu_0 \epsilon_0 \frac{\partial^2 E}{\partial t^2} \quad \text{and} \quad \frac{\partial^2 B}{\partial x^2} = \mu_0 \epsilon_0 \frac{\partial^2 B}{\partial t^2}$$

- These are in the form of a general wave equation, with

$$v = c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

- Substituting the values for  $\mu_0$  and  $\epsilon_0$  gives  $c = 2.99792 \times 10^8$  m/s

## E to B Ratio – Some Details

- The simplest solution to the partial differential equations is a sinusoidal wave:
  - $E = E_{\max} \cos(kx - \omega t)$
  - $B = B_{\max} \cos(kx - \omega t)$
- The angular wave number is  $k = 2\pi/\lambda$ 
  - $\lambda$  is the wavelength
- The angular frequency is  $\omega = 2\pi f$ 
  - $f$  is the wave frequency