

$$8-18 \quad V_C(t) = V_C(\infty) + [V_C(0^+) - V_C(\infty)] e^{-\frac{t}{\tau}}, \quad t \geq 0. \quad V_C(\infty) \text{ open voltage}$$

$$(c) \quad V_C(0^+) = 10V, \quad V_C(\infty) = V_{in}(t) = 20V, \quad \tau = R_{th}C = RC = 4s$$

$$V_C(t) = 20 + [10 - 20] e^{-\frac{t}{4}} = \underline{20 - 10e^{-\frac{t}{4}} (V)}, \quad t \geq 0$$

$$(d) \quad V_C(0) = -20V, \quad V_C(\infty) = V_{in}(t) = -10V, \quad \tau = R_{th}C = RC = 4s$$

$$V_C(t) = -10 + [-20 - (-10)] e^{-\frac{t}{4}} = \underline{-10 - 10e^{-\frac{t}{4}} (V)}, \quad t \geq 0$$

$$(e) \quad \text{Ohm's Law: } V_R(t) = I_C(t)R, \quad \text{KVL: } V_{in}(t) = V_R(t) + V_C(t)$$

$$I_C(t) = \frac{V_R(t)}{R} = \frac{V_{in}(t) - V_C(t)}{R} = \frac{1}{10k} [20 - (20 - 10e^{-\frac{t}{4}})] \quad (c)$$

$$= \underline{1 \times 10^{-3} e^{-\frac{t}{4}} (A)}, \quad t \geq 0$$

$$8-19 \quad I_L(t) = I_L(\infty) + [I_L(0^+) - I_L(\infty)] e^{-\frac{t}{\tau}}, \quad t \geq 0. \quad I_L(\infty) \text{ short current}$$

$$(c) \quad I_L(0^+) = -0.05A, \quad I_L(\infty) = \frac{V_{in}(\infty) - V_L(\infty)}{\frac{t}{R}} = 0.2A, \quad \tau = \frac{L}{R_{th}} = \frac{L}{R} = 2 \times 10^{-3}s$$

$$I_L(t) = 0.2 + [-0.05 - 0.2] e^{-\frac{t}{2 \times 10^{-3}}} = \underline{0.2 - 0.25e^{-500t} (A)}, \quad t \geq 0$$

$$(d) \quad I_L(0) = 0.025A, \quad I_L(\infty) = \frac{V_{in}(\infty) - V_L(\infty)}{\frac{t}{R}} = -0.1A, \quad \tau = \frac{L}{R_{th}} = \frac{L}{R} = 2 \times 10^{-3}s$$

$$I_L(t) = -0.1 + [0.025 - (-0.1)] e^{-\frac{t}{2 \times 10^{-3}}} = \underline{-0.1 + 0.125e^{-500t} (A)}, \quad t \geq 0$$

$$(e) \quad \text{KVL: } V_{in}(t) = V_R(t) + V_L(t), \quad \text{Ohm's Law: } V_R(t) = I_L(t)R$$

$$V_L(t) = V_{in}(t) - I_L(t)R = 20 - (0.2 - 0.25e^{-500t})100 \quad (c)$$

$$= \underline{25e^{-500t} (V)}, \quad t \geq 0$$

$$8-20 \quad V_C(t) = V_C(\infty) + [V_C(0^+) - V_C(\infty)] e^{-\frac{t}{\tau}}, \quad t \geq 0. \quad \tau = R_{th}C = (R_1 || R_2)C = 0.1s$$

$$V_C(\infty) = \frac{R_2}{R_1 + R_2} V_{in} = 16V$$

$$V_C(0^+) = V_C(0) = -8V$$

(c) zero-input response: $V_C(\infty) = V_{in}(t) = 0$, no source input.

$$V_{C1}(t) = V_C(t) \Big|_{V_C(\infty)=0} = V_C(0^+) e^{-\frac{t}{\tau}} = \underline{-8e^{-10t} (V)}, \quad t \geq 0$$

zero-state response: $V_C(0^+) = 0$, no initial condition.

$$V_{C2}(t) = V_C(t) \Big|_{V_C(0^+)=0} = V_C(\infty) - V_C(\infty) e^{-\frac{t}{\tau}} = \underline{16 - 16e^{-10t} (V)}, \quad t \geq 0$$

Note: $V_C(t)$ is complete response: $V_C(t) = V_{C1}(t) + V_{C2}(t)$

(d) For $0 < t \leq 0.25$, switch is closed, diagram is the same as (c).

$$V_C^I(t) = V_C^I(\infty) + [V_C^I(0^+) - V_C^I(\infty)] e^{-\frac{t}{\tau_I}} = 16 - 24e^{-10t} (V), \quad 0 \leq t \leq 0.25$$

$$I_c^I(t) = C \frac{dV_c^I(t)}{dt} = 2.5 \times 10^{-3} (240 e^{-10t}) = \underline{0.6 e^{-10t} (A)}, 0 < t \leq 0.25$$

For $0.25 < t \leq \underline{0.5}$ (or ∞), switch is open, diagram is changed.

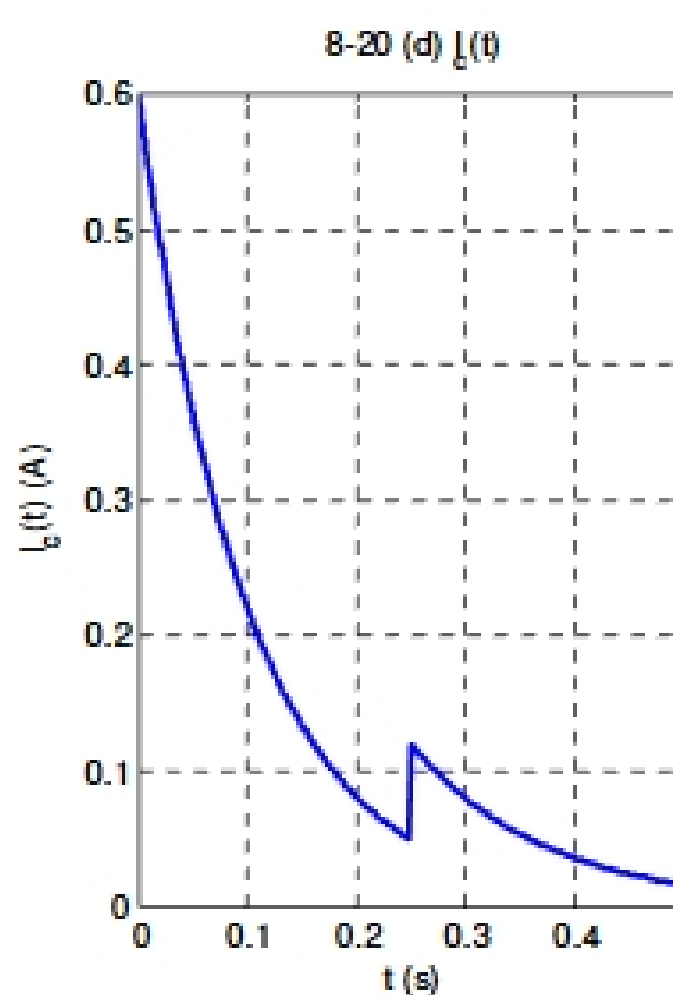
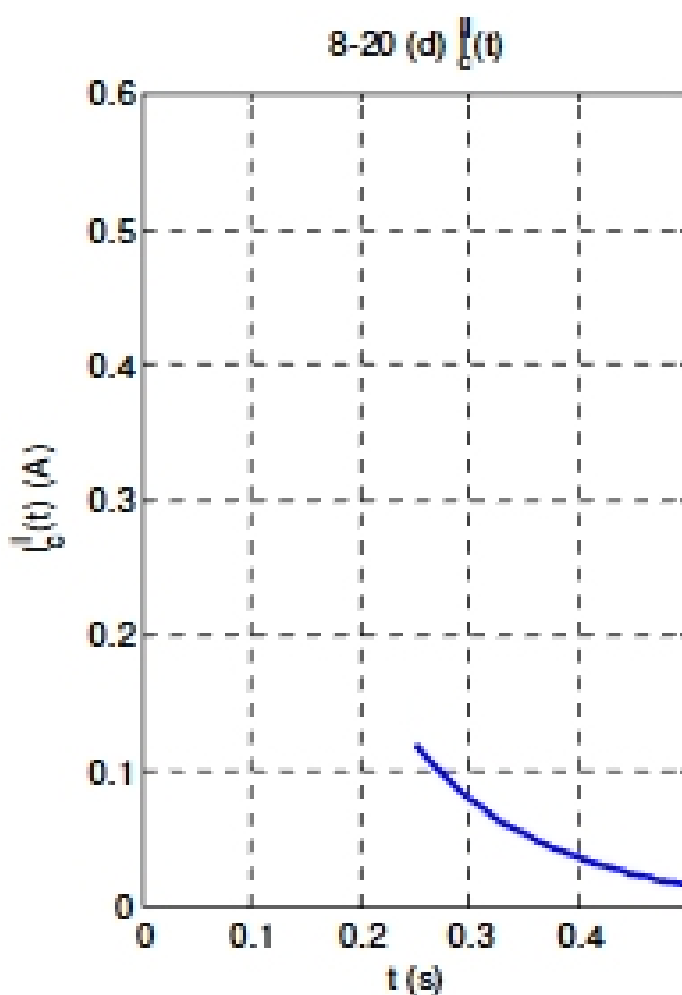
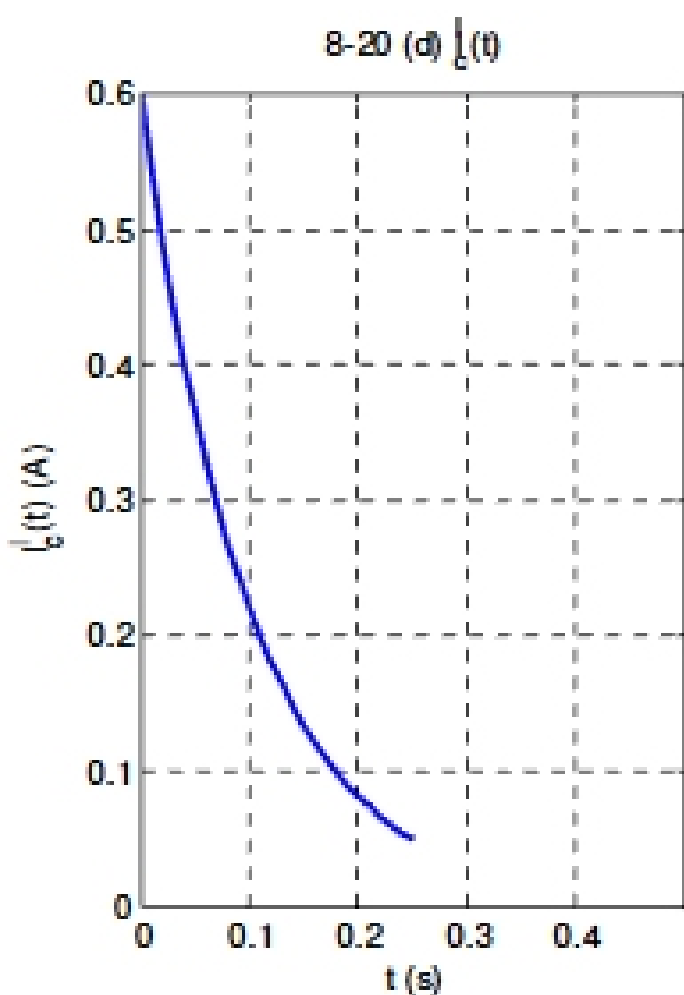
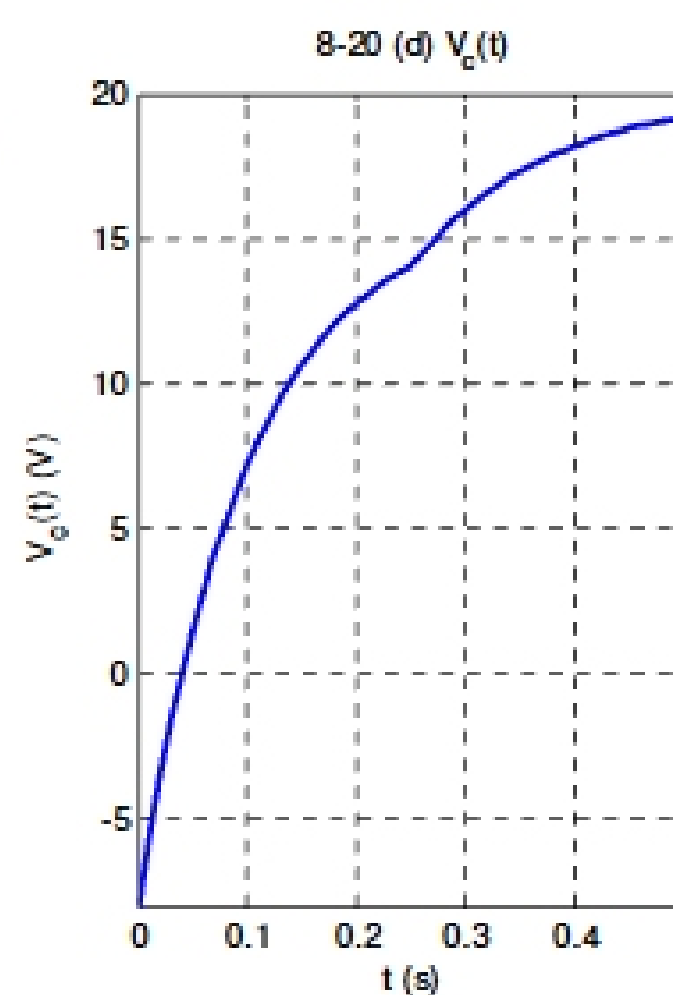
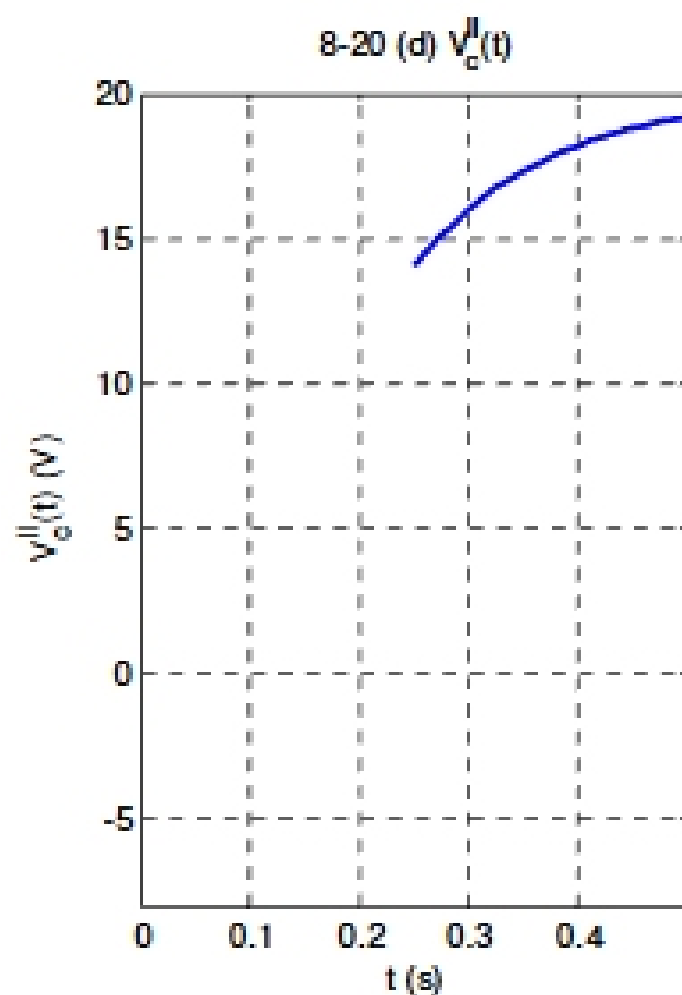
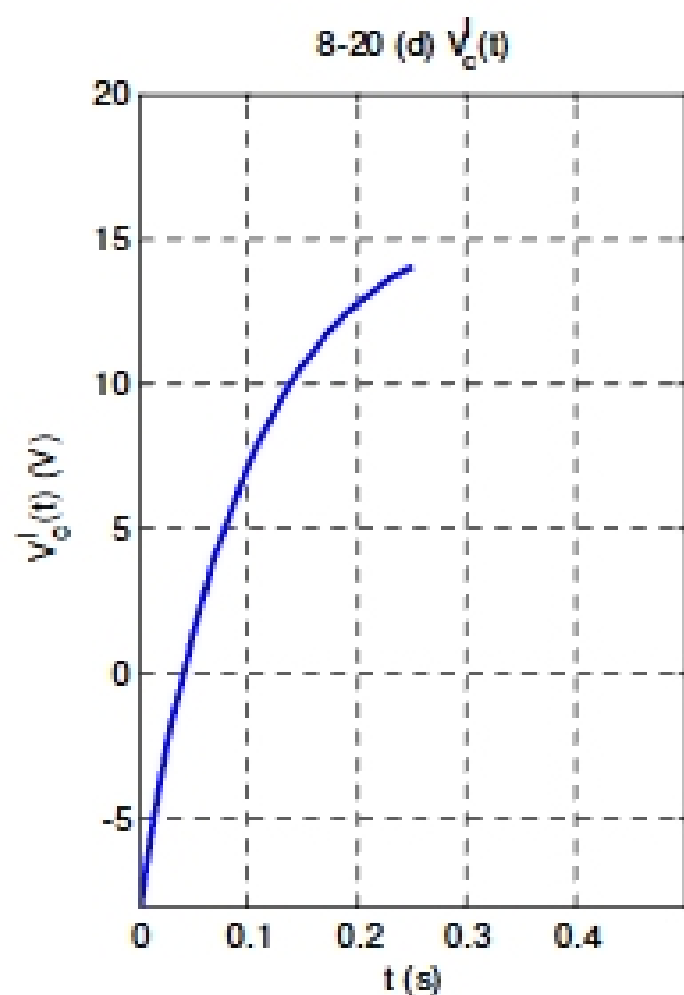
$$\tau_{II} = R_{th}^II C = R_1 C = 50 (2.5 \times 10^{-3}) = 0.125 \text{ s}, V_c(\infty) = V_{th}(\infty) = 20 \text{ V}$$

$$\text{Initial condition: } V_c^{II}(0.25^+) = V_c^I(0.25^-) = V_c^I(t) \Big|_{t=0.25} = 16 - 24e^{-2.5} = 14.03 \text{ V}$$

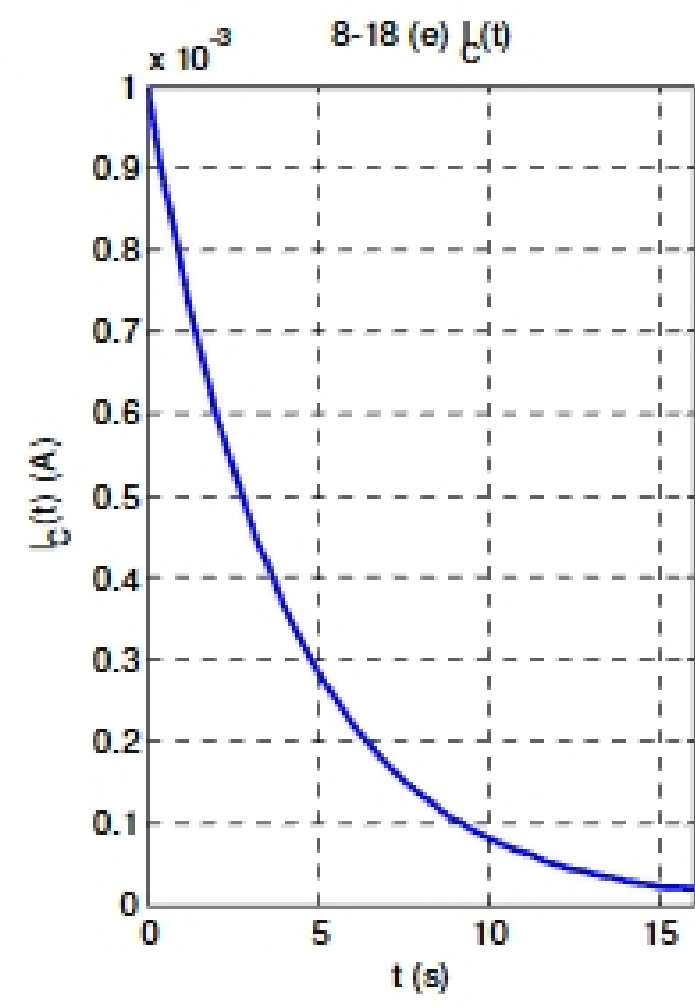
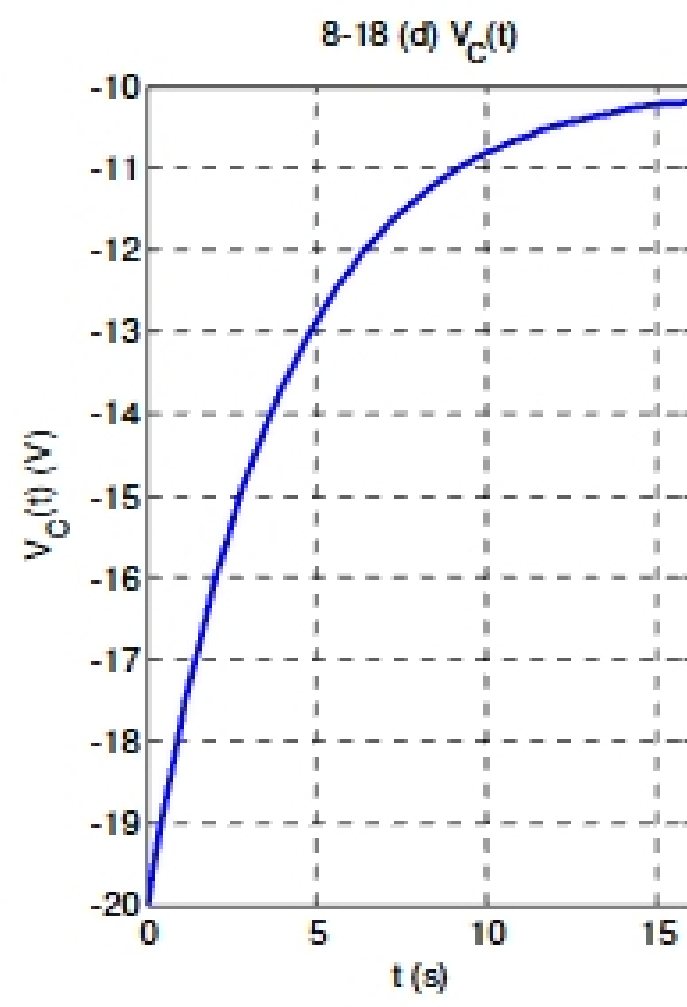
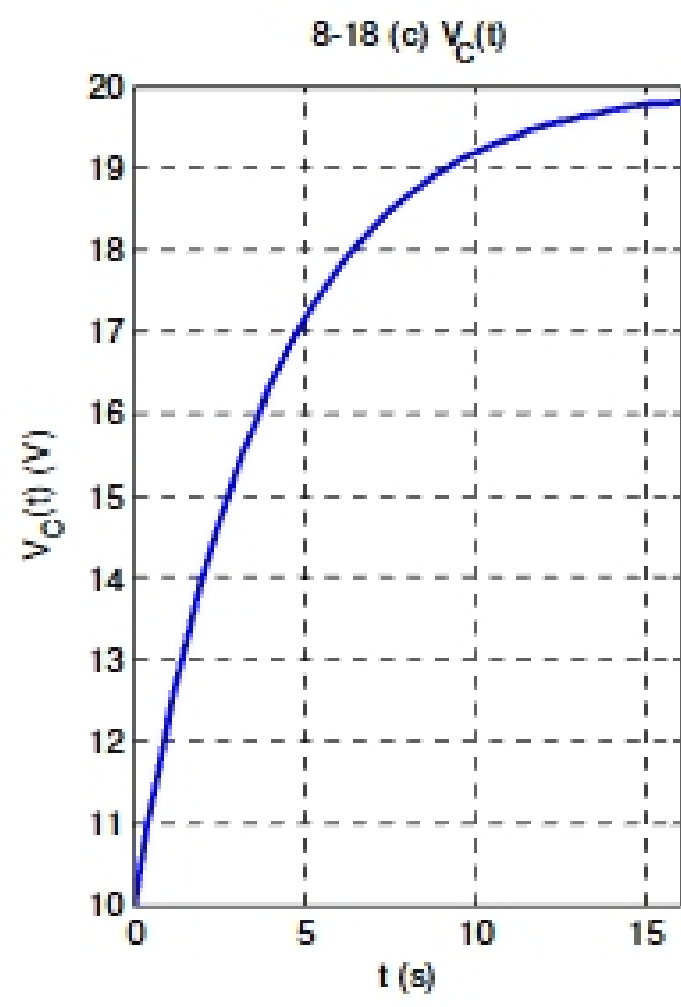
$$V_c^{II}(t) = V_c^{II}(\infty) + [V_c^{II}(0.25^+) - V_c^{II}(\infty)] e^{-\frac{t-0.25}{\tau_{II}}} = 20 - 5.97 e^{-8(t-0.25)} \text{ (V)}$$

$$I_c^{II}(t) = C \frac{dV_c^{II}(t)}{dt} = 2.5 \times 10^{-3} (47.76 e^{-8(t-0.25)}) = \underline{0.1194 e^{-8(t-0.25)} \text{ (A)}}, 0.25 < t \leq 0.5$$

$$\Rightarrow V_c(t) = \begin{cases} 16 - 24 e^{-10t} \text{ (V)}, 0 \leq t \leq 0.25 \\ 20 - 5.97 e^{-8(t-0.25)} \text{ (V)}, 0.25 < t \leq 0.5 \end{cases} \quad I_c(t) = \begin{cases} 0.6 e^{-10t} \text{ (A)}, 0 \leq t \leq 0.25 \\ 0.1194 e^{-8(t-0.25)} \text{ (A)}, 0.25 < t \leq 0.5 \end{cases}$$



8-18



8-19

