

Solving a system of equations

$$1 x_1 + 3 x_2 + 6 x_3 = 3$$

$$2 x_1 + 4 x_2 + 7 x_3 = 2$$

$$\underline{3 x_1 + 5 x_2 + 8 x_3 = 3}$$

Solving a system of equations

$$1 x_1 + 3 x_2 + 6 x_3 = 3 \quad 1$$

$$2 x_1 + 4 x_2 + 7 x_3 = 2 \quad -2$$

$$3 x_1 + 5 x_2 + 8 x_3 = 3 \quad 1$$

$$0 = 2$$

no solution

Solving a system of equations

$$a_{11} x_1 + a_{12} x_2 + a_{13} x_3 = b_1$$

$$a_{21} x_1 + a_{22} x_2 + a_{23} x_3 = b_2$$

$$a_{31} x_1 + a_{32} x_2 + a_{33} x_3 = b_3$$

$A x = b$ has a solution iff
 $\text{rank}(A) = \text{rank}(A \ b)$