

Part I

1. Find one antiderivative of $f(\theta) = e^\theta + \sec^2 \theta$.

- (A) $e^\theta + 2 \sec \theta \tan \theta$ (B) $\frac{1}{2} e^{2\theta} + \tan^2 \theta$ (C) $e^\theta + \tan \theta$
(D) $e^\theta + \tan 2\theta$ (E) $\frac{1}{2} e^{2\theta} + \tan \theta$ (F) $\ln \theta + \cos^2 \theta$
(G) $\ln \theta + \tan \theta$ (H) $\ln \theta + \tan^{-1} \theta$ (I) 1
(J) $e^\theta + \ln |\tan \theta|$

$$e^\theta + \tan \theta + C$$

2. Evaluate

$$\int_2^3 \frac{3x^2 - 1}{x^3 - x} dx.$$

(A) 0 (B) $\ln 12$ (C) $\ln 18$ (D) $\ln 4$ (E) $\ln 8$

(F) 1 (G) e^{12} (H) e^{18} (I) e^4 (J) e^8

$$\begin{aligned} u &= x^3 - x & x=2 & \quad x=3 \\ du &= (3x^2 - 1) dx & u=6 & \quad u=24 \end{aligned}$$

$$\int_6^{24} \frac{du}{u} = \ln |u| \Big|_6^{24}$$

$$= \ln 24 - \ln 6$$

$$= \ln \frac{24}{6} = \ln 4$$

3. If $f'(x) = 3x^2 + 2x + 1$ and $f(0) = 0$, find $f(2)$.

(A) 0 (B) 2 (C) 4 (D) 6 (E) 8

(F) 10 (G) 12 (H) 14 (I) 16 (J) 18

$$f(x) = x^3 + x^2 + x + C$$

$$f(0) = 0 + 0 + 0 + C = 0$$

$$C = 0$$

$$f(x) = x^3 + x^2 + x$$

$$f(2) = 8 + 4 + 2 = 14$$