

# ANOVA

## Uses of ANOVA

- Used to evaluate mean differences between two or more treatment.
- Uses sample data as basis for drawing general conclusions about populations

Advantage over multiple t test: it can be used to compare more than *two* treatments at a time

**Factor-** The independent (or quasi-independent) variable that designates the groups being compared

- Ex. Gender

**Levels-** Subdivision of factors

- Ex. Two levels for the factor of gender

**One-way ANOVA-** where the research only involves **one** factor

**Two-way ANOVA-** where the research involves **two** factors

**Factorial design-** A study that combines two or more factors

- **Null hypothesis:** In the population, the means of the groups do not differ

$$H_0 : \mu_1 = \mu_2 = \mu_3$$

from each other.

- **H<sub>1</sub>:** There is *at least one* mean difference among the populations

## ANOVA is a non-specific test

- Rejecting the null hypothesis indicates that at least one of the means is significantly different from the others
  - Doesn't say which one or if all the means are different
  - ANOVA is also called an omnibus test

$$F = \frac{\text{variance(differences) between sample means}}{\text{variance(differences) expected with no treatment effect}}$$

# ANOVA

- **Between-treatments variance (i.e., treatment variance)**
  - Variability results from general differences between the treatment conditions
  - Variance between treatments measures differences among sample means
- **Within-treatments variance (i.e., error variance)**
  - Variability within each sample
  - Individual scores are not the same within each sample
  - Variance within treatments measures expected differences under H0

1) ANOVA allows researchers to compare several treatment conditions without conducting several hypothesis tests. **TRUE**

2) If the null hypothesis is true, the  $F$ -ratio for ANOVA is expected (on average) to have a value of 0. **FALSE**

3) An analysis of variance produces  $SS_{total} = 80$  and  $SS_{within} = 30$ . For this analysis, what is  $SS_{between}$ ? **50**

4) Which combination of factors is most likely to produce a large value for the  $F$ -ratio? **large mean differences and small sample variances**

5) Post tests are needed if the decision from an analysis of variance is to fail to reject the null hypothesis. **FALSE**

6) A report shows ANOVA results:  $F(2, 27) = 5.36, p < .05$ . You can conclude that the study used a total of 30 participants **TRUE**

- Number of treatment conditions:  $k$
- Number of scores in each treatment:  $n_1, n_2, etc$
- Total number of scores:  $N$ 
  - When all samples are the same size,  $N = kn$
- Sum of scores ( $\Sigma X$ ) for each treatment:  $T$
- Grand total of all scores in study:  $G = \Sigma T$

$$F = \frac{\text{Variance between treatments}}{\text{Variance within treatments}}$$

- **There is no universally accepted notation for ANOVA. Other sources may use other symbols.**

Each variance in the  $F$ -ratio is computed as  $SS/df$

Variance between treatments =  $\frac{SS_{between}}{df_{between}}$       Variance within treatments =  $\frac{SS_{within}}{df_{within}}$

To obtain each of the  $SS$  and  $df$  values, the total variability is analyzed into the two components



## ANOVA

$$SS_{total} = \sum (X^2) - \frac{G^2}{N}$$

$$SS_{\text{between-treatments}} = \sum \left( \frac{T^2}{n} \right) - \frac{G^2}{N}$$

$$SS_{\text{within-treatments}} = \sum SS_{\text{inside each treatment}}$$

$$MS_{\text{between}} = s_{\text{between}}^2 = \frac{SS_{\text{between}}}{df_{\text{between}}}$$

$$MS_{\text{within}} = s_{\text{within}}^2 = \frac{SS_{\text{within}}}{df_{\text{within}}}$$

$$F = \frac{s_{\text{between}}^2}{s_{\text{within}}^2} = \frac{MS_{\text{between}}}{MS_{\text{within}}}$$