

The electric Potential

In this chapter we will define the electric potential (symbol V)

- Calculate V if we know the corresponding field
- Calculate the electric field if we know the electric potential

- Determine the potential V of a
 - point charge
 - continuous charge distribution

- Define the notion of an equipotential surface
- The relationship between equipotential surface and the electric field lines

Electric potential Energy:

From 107 (ch 8) you already know that the change of potential energy (ΔU) is associated with a conservative ^{delta} force, since the work W that an external force must do on a particle to take it from position x_i to a

a final position x_f

$$\Delta U = U_f - U_i = W_{\text{ext}}$$
$$= \int_{x_i}^{x_f} \vec{F}_{\text{ext}}(x) dx$$

for the electric field

$$= \ominus \int_{x_i}^{x_f} \vec{F}_E(x) dx$$

where $\vec{F}_E = q\vec{E}$ and $\vec{F}_{\text{ext}} = -\vec{F}_E$

Consider an electric charge q moving from an initial position at point A to a final position at point B in an electric field \vec{E} .

The force exerted on the charge is

$$\vec{F} = q\vec{E}$$
$$\Delta U = \int_i^f \vec{F}_{\text{ext}} \cdot d\vec{s} = - \int_i^f \vec{F}_E \cdot d\vec{s} = -q \int_i^f \vec{E} \cdot d\vec{s}$$

The electric potential V

The change in potential energy of

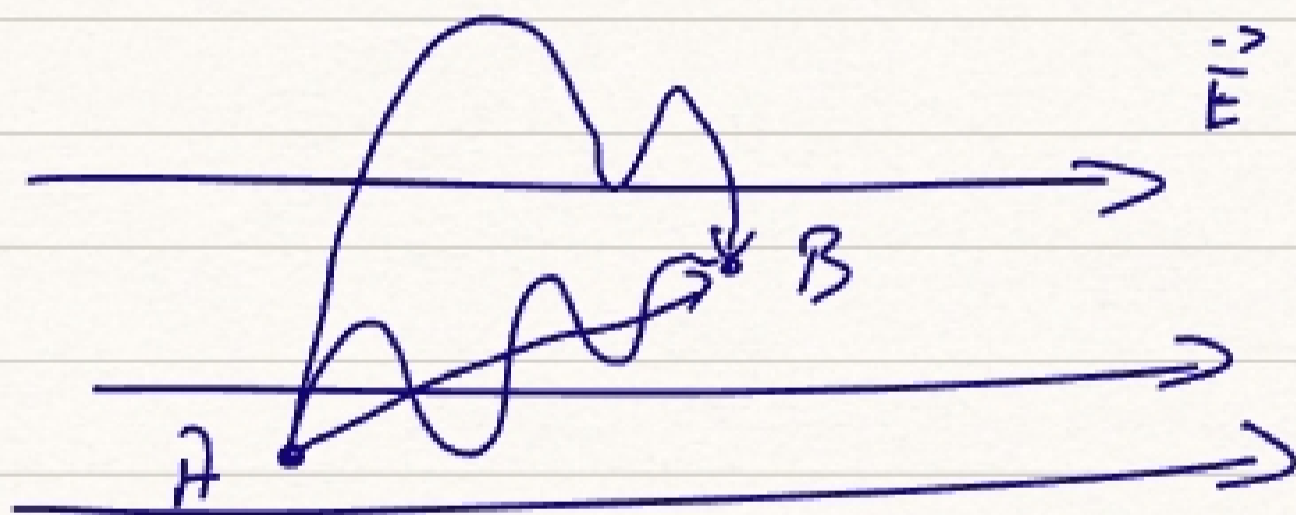
a charge q moving from A to B is

$$\Delta U = U_f - U_i = W_{\text{Ext}} = -W_E = -q \int_i^f \vec{E} \cdot d\vec{s}$$

We define the electric potential V in such a manner that it is independent of q :

$$\Delta V = \frac{\Delta U}{q} = -\frac{W_E}{q} = \frac{W_{\text{ext}}}{q}$$

$$\text{Here } \Delta V = V_f - V_i \rightarrow -\int_i^f \vec{E} \cdot d\vec{s}$$



In all physical problems only changes in V are involved. Thus we can define arbitrarily the value of V at a reference point. We choose as a reference point infinity

$$V_i = V_{\infty} = 0 \quad \text{We take the initial}$$