

Lecture Ch. 4b

- Homework Problem Ch. 4 Prob. 5
- Hydrostatic equilibrium
 - Special cases
 - Pressure altitude dependence
- More Midterm Review problems
 - Terminology review

Curry and Webster, Ch. 4 (pp. 96-115; skip 4.5, 4.6)

For Thursday: Read Ch. 5

Tuesday: Study for midterm, extra problems at end of each chapter

More Reminders

- **Virtual Temperature:** The temperature an parcel would have at the given pressure and density if there were no water vapor in it.
- **Potential Temperature:** The temperature a parcel would have if it were brought adiabatically and reversibly to P_0 (usually 1 atm).
- **Virtual Potential Temperature:** The temperature a parcel would have if there were no water vapor in it (only condensed water) and if it were brought adiabatically and reversibly to P_0 (usually 1 atm).
- **Equivalent Temperature:** The temperature that an air parcel would have if all of the water vapor were to condense in an adiabatic volume process.
- **Equivalent Potential Temperature:** The temperature a parcel would have if all of the water were condensed in an adiabatic volume process and if it were brought adiabatically and reversibly to P_0 (usually 1 atm).

Ch. 4: Problem 5

Consider moist air at a temperature of 30°C, a pressure of 1,000 hPa, and a relative humidity of 90%. Find the values of the following quantities:

- vapor pressure
- mixing ratio
- specific humidity
- specific heat at constant pressure
- virtual temperature

Hydrostatic Equilibrium Example

Consider a planet with an atmosphere in hydrostatic equilibrium. Assume that the atmosphere is an ideal gas. Also assume that the temperature is a maximum at the surface of the planet, and, as height increases, the temperature in the atmosphere decreases linearly (in other words, temperature decreases with height at a constant rate). Derive a formula for atmospheric density as a function of height in this atmosphere.

Special Cases of Hydrostatic Equilibrium

1. $\rho = \text{constant}$ (homogeneous)
 - $H = 8 \text{ km} = RT/g = \text{scale height eq. 1.39}$
 - $DT/dz = -g/R = -34 \text{ deg/km}$
2. constant lapse rate
 - $-dT/dz = \text{constant}$
3. isothermal $T = \text{constant}$
 - $p = p_0 \exp(-z/H)$

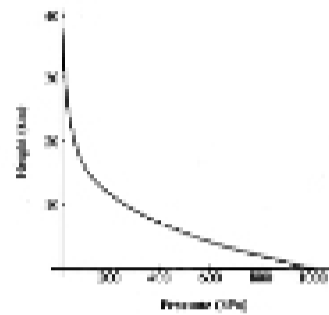
Pressure Altitude Calculator

Let's compare the hydrostatic equation to the atmosphere

$$p = p_0 \left(\frac{T}{T_0} \right)^{\beta/g} \quad T = T_0 - \Gamma z \rightarrow p = p_0 \left(\frac{T_0 - \Gamma z}{T_0} \right)^{\beta/g}$$

<http://www.cs.gsu.edu/~work.com/pressurecalc.html>

Pressure-Altitude Dependence



Latitudinal and Seasonal Variability of Pressure-Altitude

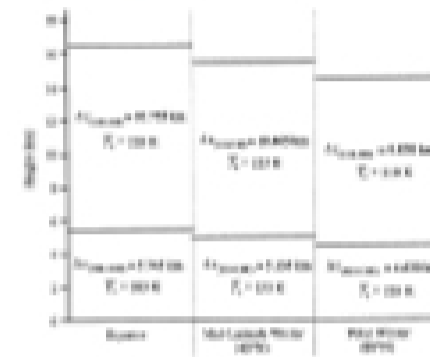


Figure 1.10: Independence of the relationship of the 1000-hPa level and 500-hPa level height and their seasonal and latitudinal variability. The relationship of the two isobars is, which is related to atmospheric structure, does not depend on the type, seasonality or the location of both of the isobars relative to each other.

Definition Example

Define the following terms, briefly and clearly, in light of their use in the kinetic theory of gases and the first and second laws of thermodynamics:

- an ideal gas
- convergence
- entropy
- exact differential
- enthalpy

Terminology Review

- **Synoptic**
 - large phenomena, hundreds of kilometers in length
- **Isentropic**
 - Adiabatic+reversible
- **For adiabatic, ideal:**
 - p determines T and vice versa
- **Potential temperature**
 - temperature that air would have if raised/lowered to a reference pressure.