

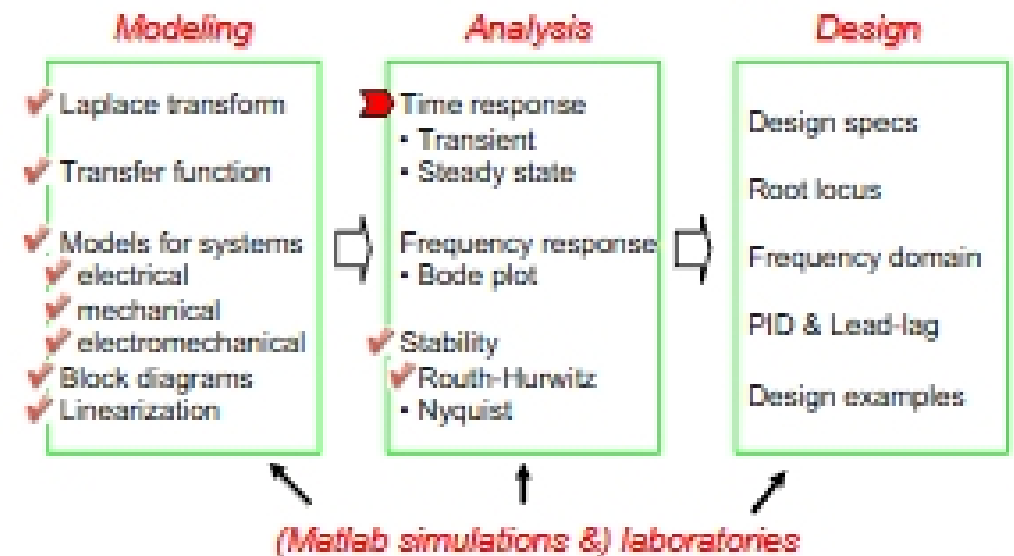
ME451: Control Systems

Lecture 12 Time-domain specifications

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Course roadmap



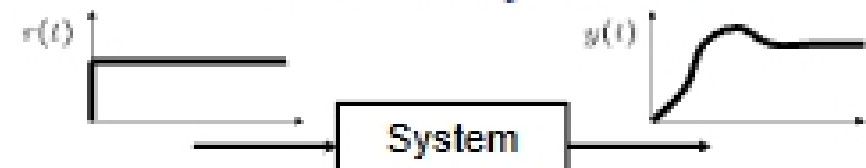
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What we do next

- We learned stability.
 - Definition in time domain
 - Condition in s-domain
 - Routh-Hurwitz criterion to check the condition
- Stability is a necessary requirement, but not sufficient in most control problems.
- Specifications other than stability
 - How to evaluate a system quantitatively in time domain?
 - How to give specifications in time domain?
 - What are the corresponding conditions in s-domain?

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Time response



- We would like to analyze a system property by applying a **test input** $r(t)$ and observing a time response $y(t)$.
- Time response is divided as

$$y(t) = \underbrace{y_t(t)} + \underbrace{y_{ss}(t)}$$

Transient response

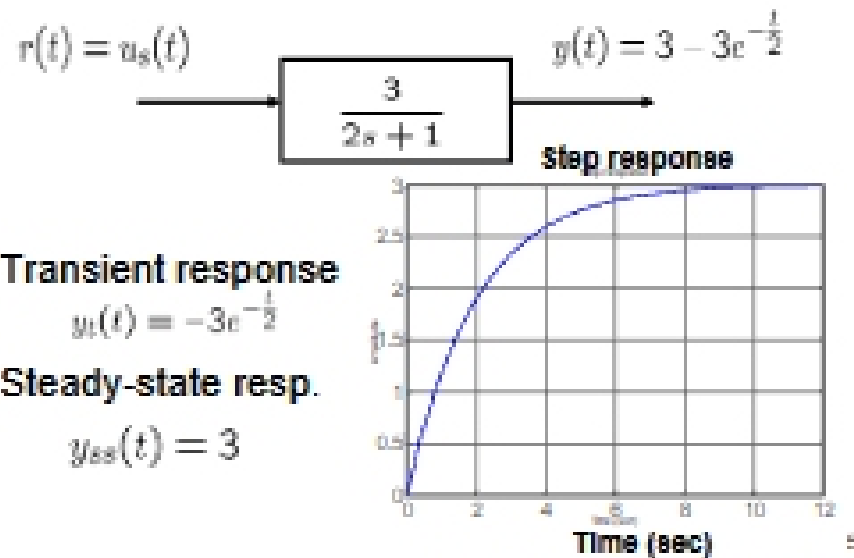
$$\lim_{t \rightarrow \infty} y_t(t) = 0$$

Steady-state response

(after y_t dies out)

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Example of transient & steady-state responses



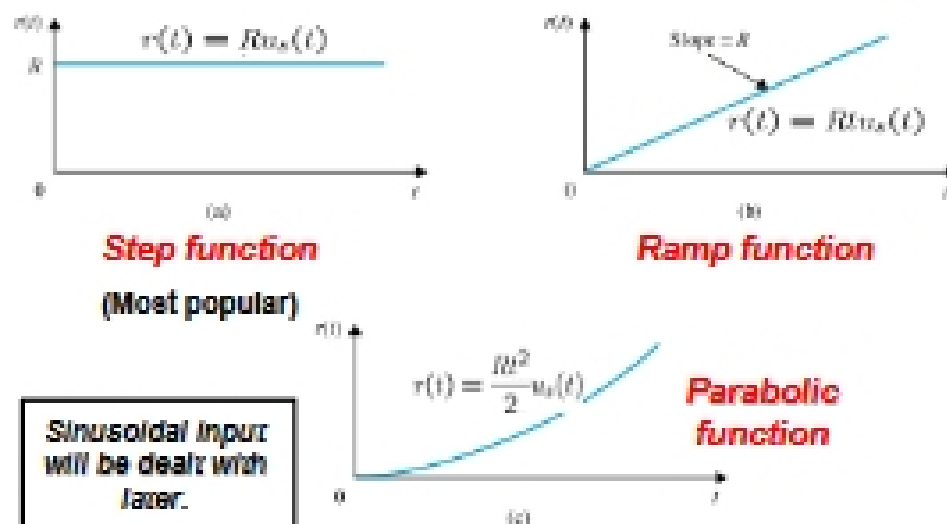
- Transient response
- Steady-state resp.

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Usage of time responses

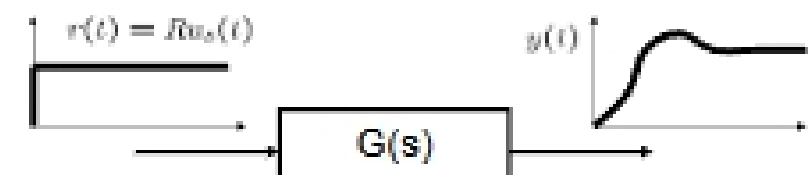
- Modeling
 - Some parameters in the system may be estimated by time responses.
- Analysis
 - Evaluate transient and steady-state responses (Satisfactory or not?)
- Design
 - Given design specs in terms of transient and steady-state responses, design controllers satisfying all the design specs.

Typical test inputs



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Steady state value for step test signal

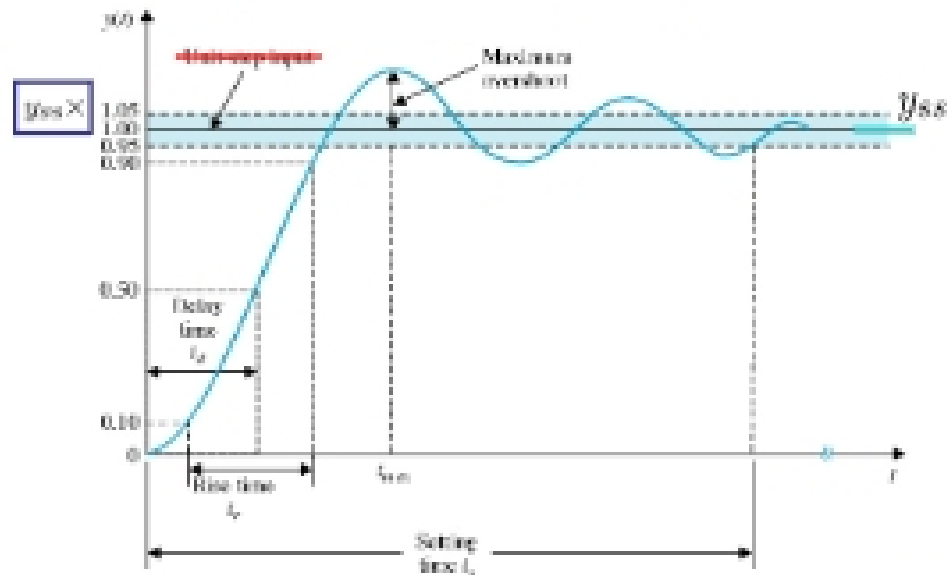


- Suppose that $G(s)$ is stable.
- By the final value theorem:

$$y(t) = \lim_{s \rightarrow 0} sG(s) \frac{R}{s} = RG(0)$$
- Step response converges to some finite value, called **steady state value** y_{ss} .

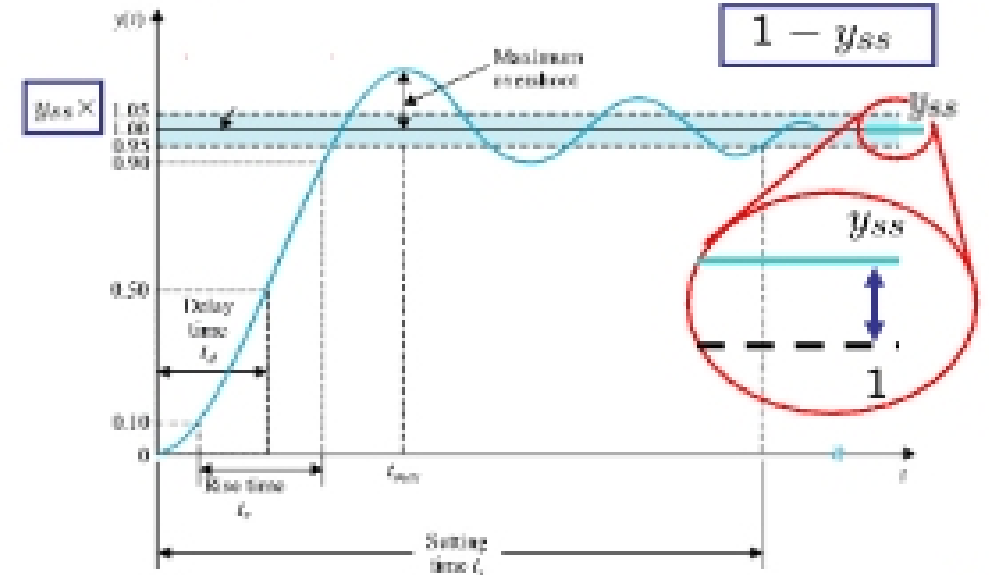
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Typical unit step response



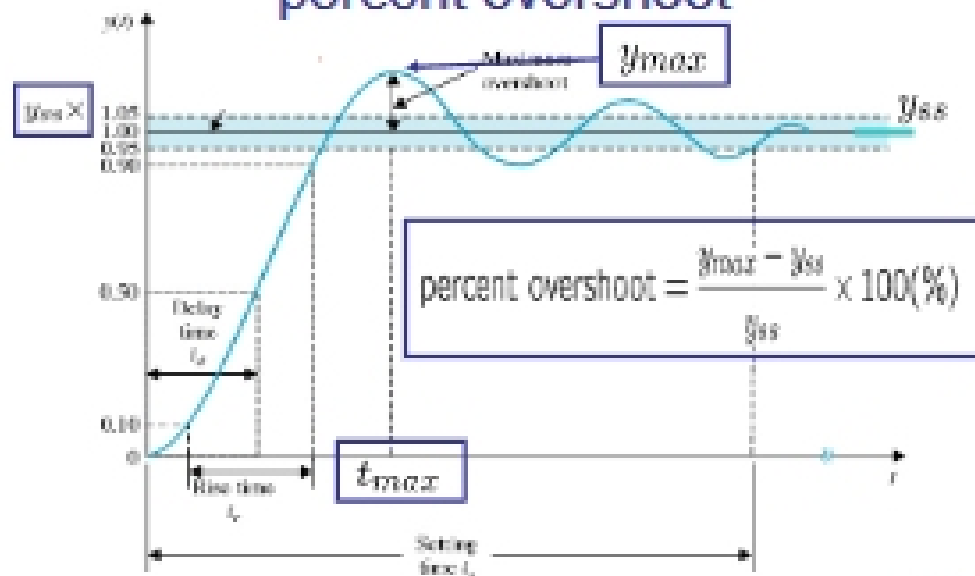
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Steady-state error for reference $u_s(t)$



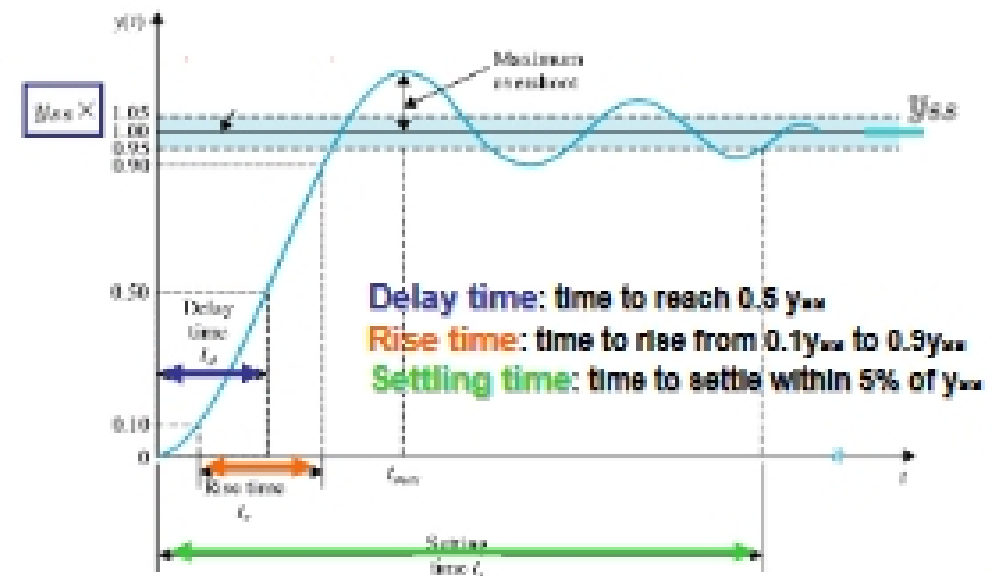
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Peak value, peak time, and percent overshoot



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Delay, rise, and settling times



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